

Maple 2018.2 Integration Test Results
on the problems in "2 Exponentials"

Test results for the 27 problems in "2.1 u (F^(c (a+b x)))^n.txt"

Problem 1: Unable to integrate problem.

$$\int F^{c(bx+a)} (ex+d)^m dx$$

Optimal(type 4, 67 leaves, 1 step):

$$\frac{F^{c\left(a-\frac{bd}{e}\right)} (ex+d)^m \Gamma\left(1+m, -\frac{bc(ex+d)\ln(F)}{e}\right)}{bc\ln(F) \left(-\frac{bc(ex+d)\ln(F)}{e}\right)^m}$$

Result(type 8, 19 leaves):

$$\int F^{c(bx+a)} (ex+d)^m dx$$

Problem 9: Unable to integrate problem.

$$\int F^{c(bx+a)} ((ex+d)^n)^m dx$$

Optimal(type 4, 73 leaves, 2 steps):

$$\frac{F^{c\left(a-\frac{bd}{e}\right)} ((ex+d)^n)^m \Gamma\left(mn+1, -\frac{bc(ex+d)\ln(F)}{e}\right)}{bc\ln(F) \left(-\frac{bc(ex+d)\ln(F)}{e}\right)^{mn}}$$

Result(type 8, 21 leaves):

$$\int F^{c(bx+a)} ((ex+d)^n)^m dx$$

Problem 10: Unable to integrate problem.

$$\int F^{c(bx+a)} (ex+d)^m dx$$

Optimal(type 4, 67 leaves, 1 step):

$$\frac{F^{c\left(a-\frac{bd}{e}\right)} (ex+d)^m \Gamma\left(1+m, -\frac{bc(ex+d)\ln(F)}{e}\right)}{bc\ln(F) \left(-\frac{bc(ex+d)\ln(F)}{e}\right)^m}$$

Result(type 8, 19 leaves):

$$\int F^{c(bx+a)} (ex+d)^m dx$$

Problem 13: Unable to integrate problem.

$$\int F^{c(bx+a)} (ex+d)^{7/2} dx$$

Optimal(type 4, 172 leaves, 6 steps):

$$\frac{35 e^2 F^{c(bx+a)} (ex+d)^{3/2}}{4 b^3 c^3 \ln(F)^3} - \frac{7 e F^{c(bx+a)} (ex+d)^{5/2}}{2 b^2 c^2 \ln(F)^2} + \frac{F^{c(bx+a)} (ex+d)^{7/2}}{b c \ln(F)} + \frac{105 e^{7/2} F^{c\left(a-\frac{bd}{e}\right)} \operatorname{erfi}\left(\frac{\sqrt{b} \sqrt{c} \sqrt{ex+d} \sqrt{\ln(F)}}{\sqrt{e}}\right) \sqrt{\pi}}{16 b^9 /2 c^9 /2 \ln(F)^9 /2} - \frac{105 e^3 F^{c(bx+a)} \sqrt{ex+d}}{8 b^4 c^4 \ln(F)^4}$$

Result(type 8, 19 leaves):

$$\int F^{c(bx+a)} (ex+d)^{7/2} dx$$

Problem 14: Unable to integrate problem.

$$\int F^{c(bx+a)} (ex+d)^{3/2} dx$$

Optimal(type 4, 110 leaves, 4 steps):

$$\frac{F^{c(bx+a)} (ex+d)^{3/2}}{b c \ln(F)} + \frac{3 e^3 /2 F^{c\left(a-\frac{bd}{e}\right)} \operatorname{erfi}\left(\frac{\sqrt{b} \sqrt{c} \sqrt{ex+d} \sqrt{\ln(F)}}{\sqrt{e}}\right) \sqrt{\pi}}{4 b^5 /2 c^5 /2 \ln(F)^5 /2} - \frac{3 e F^{c(bx+a)} \sqrt{ex+d}}{2 b^2 c^2 \ln(F)^2}$$

Result(type 8, 19 leaves):

$$\int F^{c(bx+a)} (ex+d)^{3/2} dx$$

Problem 15: Unable to integrate problem.

$$\int \frac{F^{c(bx+a)}}{(ex+d)^{5/2}} dx$$

Optimal(type 4, 100 leaves, 4 steps):

$$-\frac{2 F^{c(bx+a)}}{3 e (ex+d)^{3/2}} + \frac{4 b^3 /2 c^3 /2 F^{c\left(a-\frac{bd}{e}\right)} \operatorname{erfi}\left(\frac{\sqrt{b} \sqrt{c} \sqrt{ex+d} \sqrt{\ln(F)}}{\sqrt{e}}\right) \ln(F)^{3/2} \sqrt{\pi}}{3 e^5 /2} - \frac{4 b c F^{c(bx+a)} \ln(F)}{3 e^2 \sqrt{ex+d}}$$

Result(type 8, 19 leaves):

$$\int \frac{F^{c(bx+a)}}{(ex+d)^5 \sqrt{2}} dx$$

Problem 16: Unable to integrate problem.

$$\int \frac{F^{c(bx+a)}}{(ex+d)^9 \sqrt{2}} dx$$

Optimal(type 4, 162 leaves, 6 steps):

$$\begin{aligned} & -\frac{2F^{c(bx+a)}}{7e(ex+d)^7 \sqrt{2}} - \frac{4bcF^{c(bx+a)} \ln(F)}{35e^2(ex+d)^5 \sqrt{2}} - \frac{8b^2c^2F^{c(bx+a)} \ln(F)^2}{105e^3(ex+d)^3 \sqrt{2}} + \frac{16b^7 \sqrt{2} c^7 \sqrt{2} F^{c\left(a - \frac{bd}{e}\right)} \operatorname{erfi}\left(\frac{\sqrt{b}\sqrt{c}\sqrt{ex+d}\sqrt{\ln(F)}}{\sqrt{e}}\right) \ln(F)^7 \sqrt{2} \sqrt{\pi}}{105e^9 \sqrt{2}} \\ & - \frac{16b^3c^3F^{c(bx+a)} \ln(F)^3}{105e^4\sqrt{ex+d}} \end{aligned}$$

Result(type 8, 19 leaves):

$$\int \frac{F^{c(bx+a)}}{(ex+d)^9 \sqrt{2}} dx$$

Problem 17: Unable to integrate problem.

$$\int F^{c(bx+a)} (ex+d)^4 \sqrt[3]{2} dx$$

Optimal(type 4, 65 leaves, 1 step):

$$-\frac{eF^{c\left(a - \frac{bd}{e}\right)} (ex+d)^{1/3} \Gamma\left(\frac{7}{3}, -\frac{bc(ex+d)\ln(F)}{e}\right)}{b^2c^2\ln(F)^2 \left(-\frac{bc(ex+d)\ln(F)}{e}\right)^{1/3}}$$

Result(type 8, 19 leaves):

$$\int F^{c(bx+a)} (ex+d)^4 \sqrt[3]{2} dx$$

Problem 20: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)} x^m (fx+e)^2 dx$$

Optimal(type 4, 139 leaves, 5 steps):

$$\frac{f^2 F^{bc+a} x^m \Gamma(3+m, -bdx \ln(F))}{b^3 d^3 \ln(F)^3 (-bdx \ln(F))^m} - \frac{2efF^{bc+a} x^m \Gamma(2+m, -bdx \ln(F))}{b^2 d^2 \ln(F)^2 (-bdx \ln(F))^m} + \frac{e^2 F^{bc+a} x^m \Gamma(1+m, -bdx \ln(F))}{bd \ln(F) (-bdx \ln(F))^m}$$

Result(type 4, 432 leaves):

$$\begin{aligned}
& -\frac{1}{d^3 b^3} (\ln(F)^{-3-m} (-db)^{-m} F^{b^c+a} f^2 (x^m (-db)^m \ln(F)^m m (m^2 + 3m + 2) \Gamma(m) (-bdx \ln(F))^{-m} - x^m (-db)^m \ln(F)^m (b^2 d^2 x^2 \ln(F)^2 - mbdx \ln(F) \\
& \quad + m^2 - 2bdx \ln(F) + 3m + 2) e^{bdx \ln(F)} - x^m (-db)^m \ln(F)^m m (m^2 + 3m + 2) (-bdx \ln(F))^{-m} \Gamma(m, -bdx \ln(F))) \\
& + \frac{1}{d^2 b^2} (2 \ln(F)^{-m-2} (-db)^{-m} F^{b^c+a} f e (x^m (-db)^m \ln(F)^m (1+m) m \Gamma(m) (-bdx \ln(F))^{-m} + x^m (-db)^m \ln(F)^m (bdx \ln(F) - m - 1) e^{bdx \ln(F)} \\
& \quad - x^m (-db)^m \ln(F)^m (1+m) m (-bdx \ln(F))^{-m} \Gamma(m, -bdx \ln(F))) - \frac{1}{db} (F^{b^c+a} (-db)^{-m} \ln(F)^{-m-1} e^2 (x^m (-db)^m \ln(F)^m \Gamma(m) (-bdx \ln(F))^{-m} \\
& \quad - x^m (-db)^m \ln(F)^m e^{bdx \ln(F)} - x^m (-db)^m \ln(F)^m m (-bdx \ln(F))^{-m} \Gamma(m, -bdx \ln(F)))
\end{aligned}$$

Test results for the 27 problems in "2.2 (c+d x)^m (F^(g (e+f x)))^n (a+b (F^(g (e+f x)))^n)^p.txt"

Problem 2: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{a + b e^{dx+c}} dx$$

Optimal(type 4, 54 leaves, 4 steps):

$$\frac{x^2}{2a} - \frac{x \ln\left(1 + \frac{b e^{dx+c}}{a}\right)}{ad} - \frac{\text{polylog}\left(2, -\frac{b e^{dx+c}}{a}\right)}{a d^2}$$

Result(type 4, 132 leaves):

$$\frac{x^2}{2a} + \frac{xc}{da} + \frac{c^2}{2d^2 a} - \frac{x \ln\left(1 + \frac{b e^{dx+c}}{a}\right)}{ad} - \frac{c \ln\left(1 + \frac{b e^{dx+c}}{a}\right)}{d^2 a} - \frac{\text{polylog}\left(2, -\frac{b e^{dx+c}}{a}\right)}{a d^2} - \frac{c \ln(e^{dx+c})}{d^2 a} + \frac{c \ln(a + b e^{dx+c})}{d^2 a}$$

Problem 4: Result more than twice size of optimal antiderivative.

$$\int \frac{x^2}{(a + b e^{dx+c})^2} dx$$

Optimal(type 4, 157 leaves, 11 steps):

$$\begin{aligned}
& -\frac{x^2}{a^2 d} + \frac{x^2}{ad(a + b e^{dx+c})} + \frac{x^3}{3a^2} + \frac{2x \ln\left(1 + \frac{b e^{dx+c}}{a}\right)}{a^2 d^2} - \frac{x^2 \ln\left(1 + \frac{b e^{dx+c}}{a}\right)}{a^2 d} + \frac{2 \text{polylog}\left(2, -\frac{b e^{dx+c}}{a}\right)}{a^2 d^3} - \frac{2x \text{polylog}\left(2, -\frac{b e^{dx+c}}{a}\right)}{a^2 d^2} \\
& + \frac{2 \text{polylog}\left(3, -\frac{b e^{dx+c}}{a}\right)}{a^2 d^3}
\end{aligned}$$

Result(type 4, 323 leaves):

$$\begin{aligned}
& \frac{x^2}{ad(a+be^{dx+c})} + \frac{c^2 \ln(e^{dx+c})}{a^2 d^3} - \frac{c^2 \ln(a+be^{dx+c})}{a^2 d^3} + \frac{x^3}{3a^2} - \frac{c^2 x}{a^2 d^2} - \frac{2c^3}{3a^2 d^3} - \frac{x^2 \ln\left(1 + \frac{be^{dx+c}}{a}\right)}{a^2 d} + \frac{\ln\left(1 + \frac{be^{dx+c}}{a}\right) c^2}{a^2 d^3} \\
& - \frac{2x \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a}\right)}{a^2 d^2} + \frac{2 \operatorname{polylog}\left(3, -\frac{be^{dx+c}}{a}\right)}{a^2 d^3} + \frac{2c \ln(e^{dx+c})}{a^2 d^3} - \frac{2c \ln(a+be^{dx+c})}{a^2 d^3} - \frac{x^2}{a^2 d} - \frac{2cx}{a^2 d^2} - \frac{c^2}{a^2 d^3} + \frac{2x \ln\left(1 + \frac{be^{dx+c}}{a}\right)}{a^2 d^2} \\
& + \frac{2 \ln\left(1 + \frac{be^{dx+c}}{a}\right) c}{a^2 d^3} + \frac{2 \operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a}\right)}{a^2 d^3}
\end{aligned}$$

Problem 9: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{(a+be^{dx+c})^3} dx$$

Optimal(type 4, 143 leaves, 15 steps):

$$\begin{aligned}
& -\frac{1}{2a^2 d^2 (a+be^{dx+c})} - \frac{3x}{2a^3 d} + \frac{x}{2ad(a+be^{dx+c})^2} + \frac{x}{a^2 d(a+be^{dx+c})} + \frac{x^2}{2a^3} + \frac{3 \ln(a+be^{dx+c})}{2a^3 d^2} - \frac{x \ln\left(1 + \frac{be^{dx+c}}{a}\right)}{a^3 d} \\
& - \frac{\operatorname{polylog}\left(2, -\frac{be^{dx+c}}{a}\right)}{a^3 d^2}
\end{aligned}$$

Result(type 4, 392 leaves):

$$\begin{aligned}
& -\frac{1}{2a^2 d^2 (a+be^{dx+c})} + \frac{3 \ln(a+be^{dx+c})}{2a^3 d^2} - \frac{b^2 (e^{dx+c})^2 x}{2da^3 (a+be^{dx+c})^2} - \frac{b^2 (e^{dx+c})^2 c}{2d^2 a^3 (a+be^{dx+c})^2} - \frac{be^{dx+c} x}{da^2 (a+be^{dx+c})^2} - \frac{be^{dx+c} c}{d^2 a^2 (a+be^{dx+c})^2} + \frac{x^2}{2a^3} \\
& + \frac{xc}{da^3} + \frac{c^2}{2d^2 a^3} - \frac{be^{dx+c} x}{da^3 (a+be^{dx+c})} - \frac{be^{dx+c} c}{d^2 a^3 (a+be^{dx+c})} - \frac{\operatorname{dilog}\left(\frac{a+be^{dx+c}}{a}\right)}{d^2 a^3} - \frac{\ln\left(\frac{a+be^{dx+c}}{a}\right) x}{da^3} - \frac{\ln\left(\frac{a+be^{dx+c}}{a}\right) c}{d^2 a^3} \\
& - \frac{c \ln(e^{dx+c})}{d^2 a^3} + \frac{c \ln(a+be^{dx+c})}{d^2 a^3} - \frac{c}{d^2 a^2 (a+be^{dx+c})} - \frac{c}{2d^2 a (a+be^{dx+c})^2}
\end{aligned}$$

Problem 11: Unable to integrate problem.

$$\int \frac{a+b(Fg(fx+e))^n}{dx+c} dx$$

Optimal(type 4, 68 leaves, 4 steps):

$$\frac{b F^{\left(e - \frac{fc}{d}\right) g n - g n (fx+e)} (F^{fgx+eg})^n \operatorname{Ei}\left(\frac{fgn(dx+c)\ln(F)}{d}\right)}{d} + \frac{a \ln(dx+c)}{d}$$

Result(type 8, 25 leaves):

$$\int \frac{a + b (F^g (fx+e))^n}{dx+c} dx$$

Problem 13: Unable to integrate problem.

$$\int (a + b (F^g (fx+e))^n)^3 (dx+c)^3 dx$$

Optimal(type 3, 478 leaves, 14 steps):

$$\begin{aligned} & \frac{a^3 (dx+c)^4}{4d} - \frac{18 a^2 b d^3 (F^{fgx+eg})^n}{f^4 g^4 n^4 \ln(F)^4} - \frac{9 a b^2 d^3 (F^{fgx+eg})^{2n}}{8 f^4 g^4 n^4 \ln(F)^4} - \frac{2 b^3 d^3 (F^{fgx+eg})^{3n}}{27 f^4 g^4 n^4 \ln(F)^4} + \frac{18 a^2 b d^2 (F^{fgx+eg})^n (dx+c)}{f^3 g^3 n^3 \ln(F)^3} \\ & + \frac{9 a b^2 d^2 (F^{fgx+eg})^{2n} (dx+c)}{4 f^3 g^3 n^3 \ln(F)^3} + \frac{2 b^3 d^2 (F^{fgx+eg})^{3n} (dx+c)}{9 f^3 g^3 n^3 \ln(F)^3} - \frac{9 a^2 b d (F^{fgx+eg})^n (dx+c)^2}{f^2 g^2 n^2 \ln(F)^2} - \frac{9 a b^2 d (F^{fgx+eg})^{2n} (dx+c)^2}{4 f^2 g^2 n^2 \ln(F)^2} \\ & - \frac{b^3 d (F^{fgx+eg})^{3n} (dx+c)^2}{3 f^2 g^2 n^2 \ln(F)^2} + \frac{3 a^2 b (F^{fgx+eg})^n (dx+c)^3}{fgn \ln(F)} + \frac{3 a b^2 (F^{fgx+eg})^{2n} (dx+c)^3}{2 fgn \ln(F)} + \frac{b^3 (F^{fgx+eg})^{3n} (dx+c)^3}{3 fgn \ln(F)} \end{aligned}$$

Result(type 8, 27 leaves):

$$\int (a + b (F^g (fx+e))^n)^3 (dx+c)^3 dx$$

Problem 14: Unable to integrate problem.

$$\int (a + b (F^g (fx+e))^n)^3 (dx+c) dx$$

Optimal(type 3, 226 leaves, 8 steps):

$$\begin{aligned} & \frac{a^3 (dx+c)^2}{2d} - \frac{3 a^2 b d (F^{fgx+eg})^n}{f^2 g^2 n^2 \ln(F)^2} - \frac{3 a b^2 d (F^{fgx+eg})^{2n}}{4 f^2 g^2 n^2 \ln(F)^2} - \frac{b^3 d (F^{fgx+eg})^{3n}}{9 f^2 g^2 n^2 \ln(F)^2} + \frac{3 a^2 b (F^{fgx+eg})^n (dx+c)}{fgn \ln(F)} + \frac{3 a b^2 (F^{fgx+eg})^{2n} (dx+c)}{2 fgn \ln(F)} \\ & + \frac{b^3 (F^{fgx+eg})^{3n} (dx+c)}{3 fgn \ln(F)} \end{aligned}$$

Result(type 8, 25 leaves):

$$\int (a + b (F^g (fx+e))^n)^3 (dx+c) dx$$

Problem 15: Unable to integrate problem.

$$\int \frac{(a + b (F^g (fx+e))^n)^3}{(dx+c)^3} dx$$

Optimal (type 4, 431 leaves, 14 steps):

$$\begin{aligned} & -\frac{a^3}{2d(dx+c)^2} - \frac{3a^2b(Ffgx+eg)^n}{2d(dx+c)^2} - \frac{3ab^2(Ffgx+eg)^{2n}}{2d(dx+c)^2} - \frac{b^3(Ffgx+eg)^{3n}}{2d(dx+c)^2} - \frac{3a^2bf(Ffgx+eg)^n g n \ln(F)}{2d^2(dx+c)} - \frac{3ab^2f(Ffgx+eg)^{2n} g n \ln(F)}{d^2(dx+c)} \\ & - \frac{3b^3f(Ffgx+eg)^{3n} g n \ln(F)}{2d^2(dx+c)} + \frac{3a^2bf^2 F^{\left(e-\frac{fc}{d}\right)gn-gn(fx+e)} (Ffgx+eg)^n g^2 n^2 \operatorname{Ei}\left(\frac{fgn(dx+c)\ln(F)}{d}\right) \ln(F)^2}{2d^3} \\ & + \frac{6ab^2f^2 F^{2\left(e-\frac{fc}{d}\right)gn-2gn(fx+e)} (Ffgx+eg)^{2n} g^2 n^2 \operatorname{Ei}\left(\frac{2fgn(dx+c)\ln(F)}{d}\right) \ln(F)^2}{d^3} \\ & + \frac{9b^3f^2 F^{3\left(e-\frac{fc}{d}\right)gn-3gn(fx+e)} (Ffgx+eg)^{3n} g^2 n^2 \operatorname{Ei}\left(\frac{3fgn(dx+c)\ln(F)}{d}\right) \ln(F)^2}{2d^3} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(a + b (F^g (fx+e))^n)^3}{(dx+c)^3} dx$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx+c)^2}{a+b(F^g(fx+e))^n} dx$$

Optimal (type 4, 143 leaves, 5 steps):

$$\frac{(dx+c)^3}{3ad} - \frac{(dx+c)^2 \ln\left(1 + \frac{b(F^g(fx+e))^n}{a}\right)}{afgn \ln(F)} - \frac{2d(dx+c) \operatorname{polylog}\left(2, -\frac{b(F^g(fx+e))^n}{a}\right)}{af^2 g^2 n^2 \ln(F)^2} + \frac{2d^2 \operatorname{polylog}\left(3, -\frac{b(F^g(fx+e))^n}{a}\right)}{af^3 g^3 n^3 \ln(F)^3}$$

Result (type 4, 1340 leaves):

$$\begin{aligned} & -\frac{d^2 (\ln(F^g(fx+e)) - g(fx+e) \ln(F))^2 \ln(a + b(F^g(fx+e))^n)}{g^3 f^3 \ln(F)^3 na} - \frac{d^2 \ln\left(1 + \frac{b(F^g(fx+e))^n}{a}\right) x^2}{gf \ln(F) na} + \frac{d^2 \ln\left(1 + \frac{b(F^g(fx+e))^n}{a}\right) e^2}{g f^3 \ln(F) na} \\ & + \frac{d^2 \ln\left(1 + \frac{b(F^g(fx+e))^n}{a}\right) (\ln(F^g(fx+e)) - g(fx+e) \ln(F))^2}{g^3 f^3 \ln(F)^3 na} + \frac{2cd (\ln(F^g(fx+e)) - g(fx+e) \ln(F)) \ln(a + b(F^g(fx+e))^n)}{g^2 f^2 \ln(F)^2 na} \\ & - \frac{2cde \ln((F^g(fx+e))^n)}{gf^2 \ln(F) na} + \frac{2cde \ln(a + b(F^g(fx+e))^n)}{gf^2 \ln(F) na} + \frac{2d^2 e (\ln(F^g(fx+e)) - g(fx+e) \ln(F)) \ln((F^g(fx+e))^n)}{g^2 f^3 \ln(F)^2 na} \end{aligned}$$

$$\begin{aligned}
& - \frac{2d^2 e (\ln(F^g (fx+e)) - g (fx+e) \ln(F)) \ln(a + b (F^g (fx+e))^n)}{g^2 f^3 \ln(F)^2 n a} - \frac{2cd (\ln(F^g (fx+e)) - g (fx+e) \ln(F)) \ln((F^g (fx+e))^n)}{g^2 f^2 \ln(F)^2 n a} \\
& - \frac{2cd \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right) e}{gf^2 \ln(F) n a} - \frac{2cd \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right) (\ln(F^g (fx+e)) - g (fx+e) \ln(F))}{g^2 f^2 \ln(F)^2 n a} \\
& + \frac{2d^2 \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right) e (\ln(F^g (fx+e)) - g (fx+e) \ln(F))}{g^2 f^3 \ln(F)^2 n a} - \frac{2cd \ln(F^g (fx+e)) x}{gf \ln(F) a} - \frac{2d^2 \ln(F^g (fx+e))^3}{3g^3 f^3 \ln(F)^3 a} + \frac{2cdxe}{fa} \\
& - \frac{2d^2 ex (\ln(F^g (fx+e)) - g (fx+e) \ln(F))}{gf^2 \ln(F) a} - \frac{d^2 e^2 \ln(a + b (F^g (fx+e))^n)}{gf^3 \ln(F) n a} + \frac{d^2 e^2 \ln((F^g (fx+e))^n)}{gf^3 \ln(F) n a} - \frac{2d^2 \text{polylog}\left(2, -\frac{b (F^g (fx+e))^n}{a}\right) x}{g^2 f^2 \ln(F)^2 n^2 a} \\
& - \frac{2cd \text{polylog}\left(2, -\frac{b (F^g (fx+e))^n}{a}\right)}{g^2 f^2 \ln(F)^2 n^2 a} + \frac{d^2 (\ln(F^g (fx+e)) - g (fx+e) \ln(F))^2 \ln((F^g (fx+e))^n)}{g^3 f^3 \ln(F)^3 n a} + \frac{2cdx (\ln(F^g (fx+e)) - g (fx+e) \ln(F))}{gf \ln(F) a} \\
& + \frac{d^2 x^3}{a} + \frac{2d^2 \text{polylog}\left(3, -\frac{b (F^g (fx+e))^n}{a}\right)}{af^3 g^3 n^3 \ln(F)^3} - \frac{d^2 e^2 x}{f^2 a} + \frac{2cdx^2}{a} - \frac{2cd \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right) x}{gf \ln(F) n a} + \frac{cd \ln(F^g (fx+e))^2}{g^2 f^2 \ln(F)^2 a} - \frac{2d^2 \ln(F^g (fx+e)) x^2}{gf \ln(F) a} \\
& + \frac{2d^2 \ln(F^g (fx+e))^2 x}{g^2 f^2 \ln(F)^2 a} - \frac{c^2 \ln(a + b (F^g (fx+e))^n)}{gf \ln(F) n a} - \frac{d^2 (\ln(F^g (fx+e)) - g (fx+e) \ln(F))^2 x}{g^2 f^2 \ln(F)^2 a} + \frac{c^2 \ln((F^g (fx+e))^n)}{gf \ln(F) n a}
\end{aligned}$$

Problem 19: Result more than twice size of optimal antiderivative.

$$\int \frac{(dx+c)^2}{(a+b(F^g(fx+e))^n)^3} dx$$

Optimal(type 4, 433 leaves, 24 steps):

$$\begin{aligned}
& \frac{(dx+c)^3}{3a^3 d} + \frac{d^2 x}{a^3 f^2 g^2 n^2 \ln(F)^2} - \frac{d(dx+c)}{a^2 f^2 (a+b(F^g(fx+e))^n) g^2 n^2 \ln(F)^2} - \frac{3(dx+c)^2}{2a^3 fg n \ln(F)} + \frac{(dx+c)^2}{2af(a+b(F^g(fx+e))^n)^2 gn \ln(F)} \\
& + \frac{(dx+c)^2}{a^2 f(a+b(F^g(fx+e))^n) gn \ln(F)} - \frac{d^2 \ln(a+b(F^g(fx+e))^n)}{a^3 f^3 g^3 n^3 \ln(F)^3} + \frac{3d(dx+c) \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right)}{a^3 f^2 g^2 n^2 \ln(F)^2} - \frac{(dx+c)^2 \ln\left(1 + \frac{b (F^g (fx+e))^n}{a}\right)}{a^3 fg n \ln(F)} \\
& + \frac{3d^2 \text{polylog}\left(2, -\frac{b (F^g (fx+e))^n}{a}\right)}{a^3 f^3 g^3 n^3 \ln(F)^3} - \frac{2d(dx+c) \text{polylog}\left(2, -\frac{b (F^g (fx+e))^n}{a}\right)}{a^3 f^2 g^2 n^2 \ln(F)^2} + \frac{2d^2 \text{polylog}\left(3, -\frac{b (F^g (fx+e))^n}{a}\right)}{a^3 f^3 g^3 n^3 \ln(F)^3}
\end{aligned}$$

Result(type 4, 1456 leaves):

$$\begin{aligned}
& - \frac{d^2 \ln(a + b (Fg^{(fx+e)})^n)}{a^3 f^3 g^3 n^3 \ln(F)^3} + \frac{3 d^2 \operatorname{polylog}\left(2, -\frac{b (Fg^{(fx+e)})^n}{a}\right)}{a^3 f^3 g^3 n^3 \ln(F)^3} + \frac{2 d^2 \operatorname{polylog}\left(3, -\frac{b (Fg^{(fx+e)})^n}{a}\right)}{a^3 f^3 g^3 n^3 \ln(F)^3} - \frac{2 c d \ln(a + b (Fg^{(fx+e)})^n) x}{\ln(F) a^3 f g n} \\
& + \frac{2 c d \ln((Fg^{(fx+e)})^n) x}{\ln(F) a^3 f g n} - \frac{2 d^2 \ln((Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)}) x}{\ln(F)^2 a^3 f^2 g^2 n} + \frac{2 d^2 \ln(a + b (Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)}) x}{\ln(F)^2 a^3 f^2 g^2 n} \\
& - \frac{2 d^2 \ln\left(1 + \frac{b (Fg^{(fx+e)})^n}{a}\right) \ln(Fg^{(fx+e)}) x}{\ln(F)^2 a^3 f^2 g^2 n} - \frac{2 c d \ln\left(1 + \frac{b (Fg^{(fx+e)})^n}{a}\right) \ln(Fg^{(fx+e)})}{\ln(F)^2 a^3 f^2 g^2 n} + \frac{2 c d \ln(a + b (Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})}{\ln(F)^2 a^3 f^2 g^2 n} \\
& - \frac{2 c d \ln((Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})}{\ln(F)^2 a^3 f^2 g^2 n} - \frac{3 d^2 \ln(a + b (Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})}{\ln(F)^3 a^3 f^3 g^3 n^2} + \frac{3 d^2 \ln\left(1 + \frac{b (Fg^{(fx+e)})^n}{a}\right) \ln(Fg^{(fx+e)})}{\ln(F)^3 a^3 f^3 g^3 n^2} \\
& - \frac{3 d^2 \ln((Fg^{(fx+e)})^n) x}{\ln(F)^2 a^3 f^2 g^2 n^2} + \frac{3 d^2 \ln((Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})}{\ln(F)^3 a^3 f^3 g^3 n^2} - \frac{2 d^2 \operatorname{polylog}\left(2, -\frac{b (Fg^{(fx+e)})^n}{a}\right) x}{\ln(F)^2 a^3 f^2 g^2 n^2} - \frac{2 c d \operatorname{polylog}\left(2, -\frac{b (Fg^{(fx+e)})^n}{a}\right)}{\ln(F)^2 a^3 f^2 g^2 n^2} \\
& - \frac{3 c d \ln((Fg^{(fx+e)})^n)}{\ln(F)^2 a^3 f^2 g^2 n^2} + \frac{3 c d \ln(a + b (Fg^{(fx+e)})^n)}{\ln(F)^2 a^3 f^2 g^2 n^2} + \frac{d^2 \ln((Fg^{(fx+e)})^n) x^2}{\ln(F) a^3 f g n} + \frac{d^2 \ln((Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})^2}{\ln(F)^3 a^3 f^3 g^3 n} \\
& - \frac{d^2 \ln(a + b (Fg^{(fx+e)})^n) x^2}{\ln(F) a^3 f g n} - \frac{d^2 \ln(a + b (Fg^{(fx+e)})^n) \ln(Fg^{(fx+e)})^2}{\ln(F)^3 a^3 f^3 g^3 n} + \frac{d^2 \ln\left(1 + \frac{b (Fg^{(fx+e)})^n}{a}\right) \ln(Fg^{(fx+e)})^2}{\ln(F)^3 a^3 f^3 g^3 n} \\
& + \frac{3 d^2 \ln(a + b (Fg^{(fx+e)})^n) x}{\ln(F)^2 a^3 f^2 g^2 n^2} - \frac{2 d^2 \ln(Fg^{(fx+e)})^3}{3 \ln(F)^3 a^3 f^3 g^3} + \frac{d c \ln(Fg^{(fx+e)})^2}{\ln(F)^2 a^3 f^2 g^2} + \frac{d^2 \ln(Fg^{(fx+e)})^2 x}{\ln(F)^2 a^3 f^2 g^2} - \frac{3 d^2 \ln(Fg^{(fx+e)})^2}{2 \ln(F)^3 a^3 f^3 g^3 n} + \frac{d^2 \ln((Fg^{(fx+e)})^n)}{\ln(F)^3 a^3 f^3 g^3 n^3} \\
& + \frac{c^2 \ln((Fg^{(fx+e)})^n)}{\ln(F) a^3 f g n} - \frac{c^2 \ln(a + b (Fg^{(fx+e)})^n)}{\ln(F) a^3 f g n} + \frac{1}{2 \ln(F)^2 a^2 f^2 g^2 n^2 (a + b (Fg^{(fx+e)})^n)^2} (2 \ln(F) b d^2 f g n x^2 (Fg^{(fx+e)})^n \\
& + 3 \ln(F) a d^2 f g n x^2 + 4 \ln(F) b c d f g n x (Fg^{(fx+e)})^n + 6 \ln(F) a c d f g n x + 2 \ln(F) b c^2 f g n (Fg^{(fx+e)})^n + 3 \ln(F) a c^2 f g n - 2 b d^2 x (Fg^{(fx+e)})^n \\
& - 2 a d^2 x - 2 b c d (Fg^{(fx+e)})^n - 2 a c d)
\end{aligned}$$

Problem 23: Unable to integrate problem.

$$\int (a + b (Fg^{(fx+e)})^n)^3 (dx + c)^m dx$$

Optimal(type 4, 340 leaves, 8 steps):

$$\frac{a^3 (dx + c)^{1+m}}{d (1+m)} + \frac{3^{-m-1} b^3 F^3 \left(e^{-\frac{fc}{d}}\right) g^{n-3} g^n (fx+e) (Ffg^{fx+eg})^{3n} (dx + c)^m \Gamma\left(1+m, -\frac{3fgn(dx+c)\ln(F)}{d}\right)}{fgn \ln(F) \left(-\frac{fgn(dx+c)\ln(F)}{d}\right)^m}$$

$$\begin{aligned}
& + \frac{3 \cdot 2^{-m-1} a b^2 F^{2\left(e-\frac{fc}{d}\right)gn-2gn(fx+e)} (Ffgx+eg)^{2n} (dx+c)^m \Gamma\left(1+m, -\frac{2fgn(dx+c)\ln(F)}{d}\right)}{fgn \ln(F) \left(-\frac{fgn(dx+c)\ln(F)}{d}\right)^m} \\
& + \frac{3 a^2 b F^{\left(e-\frac{fc}{d}\right)gn-gn(fx+e)} (Ffgx+eg)^n (dx+c)^m \Gamma\left(1+m, -\frac{fgn(dx+c)\ln(F)}{d}\right)}{fgn \ln(F) \left(-\frac{fgn(dx+c)\ln(F)}{d}\right)^m}
\end{aligned}$$

Result(type 8, 27 leaves):

$$\int (a + b (F^g(fx+e))^n)^3 (dx+c)^m dx$$

Test results for the 212 problems in "2.3 Exponential functions.txt"

Problem 7: Unable to integrate problem.

$$\int (a + b (F^{e(dx+c)})^n)^p (G^h(gx+f))^{\frac{den \ln(F)}{gh \ln(G)}} dx$$

Optimal(type 3, 80 leaves, 3 steps):

$$\frac{(a + b (F^{e(dx+c)})^n)^{1+p} (G^h(gx+f))^{\frac{den \ln(F)}{gh \ln(G)}}}{b d e (F^{e(dx+c)})^n n (1+p) \ln(F)}$$

Result(type 8, 46 leaves):

$$\int (a + b (F^{e(dx+c)})^n)^p (G^h(gx+f))^{\frac{den \ln(F)}{gh \ln(G)}} dx$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \frac{f^3 b x + a}{c + d f^2 b x + e} dx$$

Optimal(type 3, 61 leaves, 3 steps):

$$\frac{f^{bx+a-e}}{bd \ln(f)} - \frac{f^{a-\frac{3e}{2}} \arctan\left(\frac{f^{\frac{bx+\frac{e}{2}}{\sqrt{d}}}}{\sqrt{c}}\right) \sqrt{c}}{bd^3 / 2 \ln(f)}$$

Result(type 3, 170 leaves):

$$\frac{f^{\frac{bx+a}{3}}}{\left(\frac{e}{f^2}\right)^2 \left(f^{-\frac{a}{3}}\right)^2 d \ln(f) b} + \frac{\sqrt{-dc} \ln \left(f^{\frac{bx+a}{3}} - \frac{\sqrt{-dc}}{df^{-\frac{a}{3}} f^{\frac{e}{f^2}}} \right)}{2 d^2 b \ln(f) \left(f^{-\frac{a}{3}}\right)^3 \left(\frac{e}{f^2}\right)^3} - \frac{\sqrt{-dc} \ln \left(f^{\frac{bx+a}{3}} + \frac{\sqrt{-dc}}{df^{-\frac{a}{3}} f^{\frac{e}{f^2}}} \right)}{2 d^2 b \ln(f) \left(f^{-\frac{a}{3}}\right)^3 \left(\frac{e}{f^2}\right)^3}$$

Problem 15: Unable to integrate problem.

$$\int \frac{f^x x^2}{a + b f^{2x}} dx$$

Optimal(type 4, 136 leaves, 9 steps):

$$\frac{x^2 \arctan\left(\frac{f^x \sqrt{b}}{\sqrt{a}}\right)}{\ln(f) \sqrt{a} \sqrt{b}} - \frac{I x \operatorname{polylog}\left(2, \frac{-I f^x \sqrt{b}}{\sqrt{a}}\right)}{\ln(f)^2 \sqrt{a} \sqrt{b}} + \frac{I x \operatorname{polylog}\left(2, \frac{I f^x \sqrt{b}}{\sqrt{a}}\right)}{\ln(f)^2 \sqrt{a} \sqrt{b}} + \frac{I \operatorname{polylog}\left(3, \frac{-I f^x \sqrt{b}}{\sqrt{a}}\right)}{\ln(f)^3 \sqrt{a} \sqrt{b}} - \frac{I \operatorname{polylog}\left(3, \frac{I f^x \sqrt{b}}{\sqrt{a}}\right)}{\ln(f)^3 \sqrt{a} \sqrt{b}}$$

Result(type 8, 20 leaves):

$$\int \frac{f^x x^2}{a + b f^{2x}} dx$$

Problem 17: Unable to integrate problem.

$$\int \frac{f^x x^2}{(a + b f^{2x})^2} dx$$

Optimal(type 4, 241 leaves, 16 steps):

$$\frac{f^x x^2}{2 a (a + b f^{2x}) \ln(f)} - \frac{x \arctan\left(\frac{f^x \sqrt{b}}{\sqrt{a}}\right)}{a^3 / 2 \ln(f)^2 \sqrt{b}} + \frac{x^2 \arctan\left(\frac{f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f) \sqrt{b}} + \frac{I \operatorname{polylog}\left(2, \frac{-I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^3 \sqrt{b}} - \frac{I x \operatorname{polylog}\left(2, \frac{-I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^2 \sqrt{b}} - \frac{I \operatorname{polylog}\left(2, \frac{I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^3 \sqrt{b}}$$

$$+ \frac{I x \operatorname{polylog}\left(2, \frac{I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^2 \sqrt{b}} + \frac{I \operatorname{polylog}\left(3, \frac{-I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^3 \sqrt{b}} - \frac{I \operatorname{polylog}\left(3, \frac{I f^x \sqrt{b}}{\sqrt{a}}\right)}{2 a^3 / 2 \ln(f)^3 \sqrt{b}}$$

Result(type 8, 67 leaves):

$$\frac{e^{x \ln(f)} x^2}{2 \ln(f) a (a + b (e^{x \ln(f)})^2)} + \int \frac{e^{x \ln(f)} x (x \ln(f) - 2)}{2 \ln(f) a (a + b (e^{x \ln(f)})^2)} dx$$

Problem 18: Unable to integrate problem.

$$\int \frac{x^2}{\frac{b}{f^x} + a f^x} dx$$

Optimal(type 4, 136 leaves, 9 steps):

$$\frac{x^2 \arctan\left(\frac{f^x \sqrt{a}}{\sqrt{b}}\right)}{\ln(f) \sqrt{a} \sqrt{b}} - \frac{\text{Ixpolylog}\left(2, \frac{-1 f^x \sqrt{a}}{\sqrt{b}}\right)}{\ln(f)^2 \sqrt{a} \sqrt{b}} + \frac{\text{Ixpolylog}\left(2, \frac{1 f^x \sqrt{a}}{\sqrt{b}}\right)}{\ln(f)^2 \sqrt{a} \sqrt{b}} + \frac{\text{Ipolylog}\left(3, \frac{-1 f^x \sqrt{a}}{\sqrt{b}}\right)}{\ln(f)^3 \sqrt{a} \sqrt{b}} - \frac{\text{Ipolylog}\left(3, \frac{1 f^x \sqrt{a}}{\sqrt{b}}\right)}{\ln(f)^3 \sqrt{a} \sqrt{b}}$$

Result(type 8, 21 leaves):

$$\int \frac{x^2}{\frac{b}{f^x} + a f^x} dx$$

Problem 20: Unable to integrate problem.

$$\int \frac{x^2}{\left(\frac{b}{f^x} + a f^x\right)^3} dx$$

Optimal(type 4, 242 leaves, 43 steps):

$$\begin{aligned} & -\frac{\arctan\left(\frac{f^x \sqrt{a}}{\sqrt{b}}\right)}{4 a^3 / 2 b^3 / 2 \ln(f)^3} + \frac{f^x x}{4 a b (b + a f^{2x}) \ln(f)^2} - \frac{f^x x^2}{4 a (b + a f^{2x})^2 \ln(f)} + \frac{f^x x^2}{8 a b (b + a f^{2x}) \ln(f)} + \frac{x^2 \arctan\left(\frac{f^x \sqrt{a}}{\sqrt{b}}\right)}{8 a^3 / 2 b^3 / 2 \ln(f)} - \frac{\text{Ixpolylog}\left(2, \frac{-1 f^x \sqrt{a}}{\sqrt{b}}\right)}{8 a^3 / 2 b^3 / 2 \ln(f)^2} \\ & + \frac{\text{Ixpolylog}\left(2, \frac{1 f^x \sqrt{a}}{\sqrt{b}}\right)}{8 a^3 / 2 b^3 / 2 \ln(f)^2} + \frac{\text{Ipolylog}\left(3, \frac{-1 f^x \sqrt{a}}{\sqrt{b}}\right)}{8 a^3 / 2 b^3 / 2 \ln(f)^3} - \frac{\text{Ipolylog}\left(3, \frac{1 f^x \sqrt{a}}{\sqrt{b}}\right)}{8 a^3 / 2 b^3 / 2 \ln(f)^3} \end{aligned}$$

Result(type 8, 106 leaves):

$$\frac{e^{x \ln(f)} x (\ln(f) a x (e^{x \ln(f)})^2 - \ln(f) b x + 2 (e^{x \ln(f)})^2 a + 2 b)}{8 b \ln(f)^2 a ((e^{x \ln(f)})^2 a + b)^2} + \int \frac{e^{x \ln(f)} (\ln(f)^2 x^2 - 2)}{8 b \ln(f)^2 a ((e^{x \ln(f)})^2 a + b)} dx$$

Problem 21: Unable to integrate problem.

$$\int f e^{x^2 + b x + a} g^{f x^2 + e x + d} dx$$

Optimal(type 4, 84 leaves, 3 steps):

$$\frac{f^a g^d \operatorname{erfi}\left(\frac{b \ln(f) + e \ln(g) + 2x(c \ln(f) + f \ln(g))}{2\sqrt{c \ln(f) + f \ln(g)}}\right) \sqrt{\pi}}{2 e^{\frac{(b \ln(f) + e \ln(g))^2}{4(c \ln(f) + f \ln(g))}} \sqrt{c \ln(f) + f \ln(g)}}$$

Result(type 8, 27 leaves):

$$\int f^{cx^2+bx+a} g^{fx^2+ex+d} dx$$

Problem 22: Unable to integrate problem.

$$\int F^{e(dx+c)} (a + b G^{h(gx+f)})^n dx$$

Optimal(type 5, 108 leaves, 2 steps):

$$\frac{F^{e(dx+c)} (a + b G^{h(gx+f)})^n \operatorname{hypergeom}\left(\left[-n, \frac{de \ln(F)}{gh \ln(G)}\right], \left[1 + \frac{de \ln(F)}{gh \ln(G)}\right], -\frac{b G^{h(gx+f)}}{a}\right)}{de \left(1 + \frac{b G^{h(gx+f)}}{a}\right)^n \ln(F)}$$

Result(type 8, 27 leaves):

$$\int F^{e(dx+c)} (a + b G^{h(gx+f)})^n dx$$

Problem 24: Result more than twice size of optimal antiderivative.

$$\int \frac{f^b x^2 + a}{x^9} dx$$

Optimal(type 4, 18 leaves, 1 step):

$$-\frac{f^a \operatorname{Ei}_5(-bx^2 \ln(f))}{2x^8}$$

Result(type 4, 100 leaves):

$$-\frac{f^a f^b x^2}{8x^8} - \frac{f^a \ln(f) b f^b x^2}{24x^6} - \frac{f^a \ln(f)^2 b^2 f^b x^2}{48x^4} - \frac{f^a \ln(f)^3 b^3 f^b x^2}{48x^2} - \frac{f^a \ln(f)^4 b^4 \operatorname{Ei}_1(-bx^2 \ln(f))}{48}$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \frac{f^b x^2 + a}{x^{11}} dx$$

Optimal(type 4, 18 leaves, 1 step):

$$-\frac{f^a \operatorname{Ei}_6(-bx^2 \ln(f))}{2x^{10}}$$

Result(type 4, 122 leaves):

$$\frac{f^a f^b x^2}{10x^{10}} - \frac{f^a \ln(f) b f^b x^2}{40x^8} - \frac{f^a \ln(f)^2 b^2 f^b x^2}{120x^6} - \frac{f^a \ln(f)^3 b^3 f^b x^2}{240x^4} - \frac{f^a \ln(f)^4 b^4 f^b x^2}{240x^2} - \frac{f^a \ln(f)^5 b^5 \text{Ei}_1(-bx^2 \ln(f))}{240}$$

Problem 30: Result more than twice size of optimal antiderivative.

$$\int \frac{f^b x^3 + a}{x} dx$$

Optimal(type 4, 13 leaves, 1 step):

$$\frac{f^a \text{Ei}(bx^3 \ln(f))}{3}$$

Result(type 4, 40 leaves):

$$\frac{f^a \left(3 \ln(x) + \ln(-b) + \ln(\ln(f)) - \ln(-bx^3 \ln(f)) - \text{Ei}_1(-bx^3 \ln(f)) \right)}{3}$$

Problem 31: Result more than twice size of optimal antiderivative.

$$\int \frac{f^b x^3 + a}{x^3} dx$$

Optimal(type 4, 28 leaves, 1 step):

$$-\frac{f^a \Gamma\left(-\frac{2}{3}, -bx^3 \ln(f)\right) (-bx^3 \ln(f))^{2/3}}{3x^2}$$

Result(type 4, 101 leaves):

$$-\frac{f^a b \ln(f)^{2/3} \left(\frac{x \ln(f)^{1/3} b \pi \sqrt{3}}{(-b)^{2/3} \Gamma\left(\frac{2}{3}\right) (-bx^3 \ln(f))^{1/3}} - \frac{3 e^{bx^3 \ln(f)}}{2x^2 (-b)^{2/3} \ln(f)^{2/3}} - \frac{3x \ln(f)^{1/3} b \Gamma\left(\frac{1}{3}, -bx^3 \ln(f)\right)}{2(-b)^{2/3} (-bx^3 \ln(f))^{1/3}} \right)}{3(-b)^{1/3}}$$

Problem 32: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x}} x^3 dx$$

Optimal(type 4, 17 leaves, 1 step):

$$f^a x^4 \text{Ei}_5\left(-\frac{b \ln(f)}{x}\right)$$

Result(type 4, 102 leaves):

$$\frac{f^{\frac{ax+b}{x}} x^4}{4} + \frac{\ln(f) b f^{\frac{ax+b}{x}} x^3}{12} + \frac{\ln(f)^2 b^2 f^{\frac{ax+b}{x}} x^2}{24} + \frac{\ln(f)^3 b^3 f^{\frac{ax+b}{x}} x}{24} + \frac{\ln(f)^4 b^4 f^a \operatorname{Ei}_1\left(-\frac{b \ln(f)}{x}\right)}{24}$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^3}} x^{14} dx$$

Optimal (type 4, 18 leaves, 1 step):

$$\frac{f^a x^{15} \operatorname{Ei}_6\left(-\frac{b \ln(f)}{x^3}\right)}{3}$$

Result (type 4, 248 leaves):

$$\frac{1}{3} \left(f^a b^5 \ln(f)^5 \left(\frac{x^{15}}{5 b^5 \ln(f)^5} + \frac{x^{12}}{4 b^4 \ln(f)^4} + \frac{x^9}{6 b^3 \ln(f)^3} + \frac{x^6}{12 b^2 \ln(f)^2} + \frac{x^3}{24 b \ln(f)} + \frac{137}{7200} + \frac{\ln(x)}{40} - \frac{\ln(-b)}{120} - \frac{\ln(\ln(f))}{120} \right) - \frac{x^{15} \left(\frac{137 b^5 \ln(f)^5}{x^{15}} + \frac{300 b^4 \ln(f)^4}{x^{12}} + \frac{600 b^3 \ln(f)^3}{x^9} + \frac{1200 b^2 \ln(f)^2}{x^6} + \frac{1800 b \ln(f)}{x^3} + 1440 \right)}{7200 b^5 \ln(f)^5} + \frac{x^{15} \left(\frac{6 b^4 \ln(f)^4}{x^{12}} + \frac{6 b^3 \ln(f)^3}{x^9} + \frac{12 b^2 \ln(f)^2}{x^6} + \frac{36 b \ln(f)}{x^3} + 144 \right) e^{\frac{b \ln(f)}{x^3}}}{720 b^5 \ln(f)^5} + \frac{\ln\left(-\frac{b \ln(f)}{x^3}\right)}{120} + \frac{\operatorname{Ei}_1\left(-\frac{b \ln(f)}{x^3}\right)}{120} \right)$$

Problem 46: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^3}} x^{11} dx$$

Optimal (type 4, 18 leaves, 1 step):

$$\frac{f^a x^{12} \operatorname{Ei}_5\left(-\frac{b \ln(f)}{x^3}\right)}{3}$$

Result (type 4, 212 leaves):

$$-\frac{1}{3} \left(f^a b^4 \ln(f)^4 \left(-\frac{x^{12}}{4 b^4 \ln(f)^4} - \frac{x^9}{3 b^3 \ln(f)^3} - \frac{x^6}{4 b^2 \ln(f)^2} - \frac{x^3}{6 b \ln(f)} - \frac{25}{288} - \frac{\ln(x)}{8} + \frac{\ln(-b)}{24} + \frac{\ln(\ln(f))}{24} \right) \right)$$

$$+ \frac{x^{12} \left(\frac{125 b^4 \ln(f)^4}{x^{12}} + \frac{240 b^3 \ln(f)^3}{x^9} + \frac{360 b^2 \ln(f)^2}{x^6} + \frac{480 b \ln(f)}{x^3} + 360 \right) - \frac{x^{12} \left(\frac{5 b^3 \ln(f)^3}{x^9} + \frac{5 b^2 \ln(f)^2}{x^6} + \frac{10 b \ln(f)}{x^3} + 30 \right) e^{\frac{b \ln(f)}{x^3}}}{1440 b^4 \ln(f)^4} - \frac{120 b^4 \ln(f)^4}{120 b^4 \ln(f)^4} - \left. \left(\frac{\ln\left(-\frac{b \ln(f)}{x^3}\right)}{24} - \frac{\text{Ei}_1\left(-\frac{b \ln(f)}{x^3}\right)}{24} \right) \right)$$

Problem 48: Result more than twice size of optimal antiderivative.

$$\int f^{a + \frac{b}{x^3}} x^4 dx$$

Optimal(type 4, 28 leaves, 1 step):

$$\frac{f^a x^5 \Gamma\left(-\frac{5}{3}, -\frac{b \ln(f)}{x^3}\right) \left(-\frac{b \ln(f)}{x^3}\right)^{5/3}}{3}$$

Result(type 4, 119 leaves):

$$\frac{f^a (-b)^{5/3} \ln(f)^{5/3} \left(\frac{3 \ln(f)^{1/3} b^2 \pi \sqrt{3}}{5x (-b)^{5/3} \Gamma\left(\frac{2}{3}\right) \left(-\frac{b \ln(f)}{x^3}\right)^{1/3}} - \frac{3x^5 \left(\frac{3b \ln(f)}{2x^3} + 1\right) e^{\frac{b \ln(f)}{x^3}}}{5 (-b)^{5/3} \ln(f)^{5/3}} - \frac{9 \ln(f)^{1/3} b^2 \Gamma\left(\frac{1}{3}, -\frac{b \ln(f)}{x^3}\right)}{10x (-b)^{5/3} \left(-\frac{b \ln(f)}{x^3}\right)^{1/3}} \right)}{3}$$

Problem 55: Unable to integrate problem.

$$\int e^{b^3 x^3 + 3 a b^2 x^2 + 3 a^2 b x + a^3} x^4 dx$$

Optimal(type 4, 158 leaves, 8 steps):

$$\frac{2 a^2 e^{(bx+a)^3}}{b^5} - \frac{a^4 (bx+a) \Gamma\left(\frac{1}{3}, -(bx+a)^3\right)}{3 b^5 (-(bx+a)^3)^{1/3}} + \frac{4 a^3 (bx+a)^2 \Gamma\left(\frac{2}{3}, -(bx+a)^3\right)}{3 b^5 (-(bx+a)^3)^{2/3}} + \frac{4 a (bx+a)^4 \Gamma\left(\frac{4}{3}, -(bx+a)^3\right)}{3 b^5 (-(bx+a)^3)^{4/3}} - \frac{(bx+a)^5 \Gamma\left(\frac{5}{3}, -(bx+a)^3\right)}{3 b^5 (-(bx+a)^3)^{5/3}}$$

Result(type 8, 34 leaves):

$$\int e^{b^3 x^3 + 3 a b^2 x^2 + 3 a^2 b x + a^3} x^4 dx$$

Problem 63: Unable to integrate problem.

$$\int \frac{c}{f^{(bx+a)^3}} x^3 dx$$

Optimal(type 4, 168 leaves, 7 steps):

$$\begin{aligned} & -\frac{\frac{c}{af^{(bx+a)^3}} (bx+a)^3}{b^4} + \frac{ac \operatorname{Ei}\left(\frac{c \ln(f)}{(bx+a)^3}\right) \ln(f)}{b^4} - \frac{a^3 (bx+a) \Gamma\left(-\frac{1}{3}, -\frac{c \ln(f)}{(bx+a)^3}\right) \left(-\frac{c \ln(f)}{(bx+a)^3}\right)^{1/3}}{3b^4} \\ & + \frac{a^2 (bx+a)^2 \Gamma\left(-\frac{2}{3}, -\frac{c \ln(f)}{(bx+a)^3}\right) \left(-\frac{c \ln(f)}{(bx+a)^3}\right)^{2/3}}{b^4} + \frac{(bx+a)^4 \Gamma\left(-\frac{4}{3}, -\frac{c \ln(f)}{(bx+a)^3}\right) \left(-\frac{c \ln(f)}{(bx+a)^3}\right)^{4/3}}{3b^4} \end{aligned}$$

Result(type 8, 17 leaves):

$$\int \frac{c}{f^{(bx+a)^3}} x^3 dx$$

Problem 66: Result more than twice size of optimal antiderivative.

$$\int f^{(bx+a)} x^m dx$$

Optimal(type 4, 41 leaves, 1 step):

$$\frac{f^a c x^m \Gamma(1+m, -bcx \ln(f))}{bc \ln(f) (-bcx \ln(f))^m}$$

Result(type 4, 116 leaves):

$$-\frac{1}{bc} (f^a c (-bc)^{-m} \ln(f)^{-m-1} (x^m (-bc)^m \ln(f)^m m \Gamma(m) (-bcx \ln(f))^{-m} - x^m (-bc)^m \ln(f)^m e^{bcx \ln(f)} - x^m (-bc)^m \ln(f)^m m (-bcx \ln(f))^{-m} \Gamma(m, -bcx \ln(f))))$$

Problem 68: Unable to integrate problem.

$$\int f^{(bx+a)^n} x^3 dx$$

Optimal(type 4, 213 leaves, 6 steps):

$$\begin{aligned} & -\frac{(bx+a)^4 \Gamma\left(\frac{4}{n}, -c(bx+a)^n \ln(f)\right)}{b^4 n (-c(bx+a)^n \ln(f))^{\frac{4}{n}}} + \frac{3a(bx+a)^3 \Gamma\left(\frac{3}{n}, -c(bx+a)^n \ln(f)\right)}{b^4 n (-c(bx+a)^n \ln(f))^{\frac{3}{n}}} - \frac{3a^2(bx+a)^2 \Gamma\left(\frac{2}{n}, -c(bx+a)^n \ln(f)\right)}{b^4 n (-c(bx+a)^n \ln(f))^{\frac{2}{n}}} \end{aligned}$$

$$+ \frac{a^3 (bx+a) \Gamma\left(\frac{1}{n}, -c(bx+a)^n \ln(f)\right)}{b^4 n (-c(bx+a)^n \ln(f))^{\frac{1}{n}}}$$

Result(type 8, 17 leaves):

$$\int f^{c(bx+a)^n} x^3 dx$$

Problem 69: Unable to integrate problem.

$$\int f^{c(bx+a)^n} dx$$

Optimal(type 4, 47 leaves, 1 step):

$$- \frac{(bx+a) \Gamma\left(\frac{1}{n}, -c(bx+a)^n \ln(f)\right)}{bn (-c(bx+a)^n \ln(f))^{\frac{1}{n}}}$$

Result(type 8, 13 leaves):

$$\int f^{c(bx+a)^n} dx$$

Problem 73: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^2} (dx+c)^{12} dx$$

Optimal(type 4, 578 leaves, 1 step):

$$- \frac{1}{2d (-b(dx+c)^2 \ln(F))^{13} / 2} \left(F^a (dx+c)^{13} \left(\frac{524288 \Gamma\left(\frac{51}{2}, -b(dx+c)^2 \ln(F)\right)}{5621533568633696205238621875} - \frac{524288 (-b(dx+c)^2 \ln(F))^{49} / 2 e^{b(dx+c)^2 \ln(F)}}{5621533568633696205238621875} \right. \right. \\ - \frac{262144 (-b(dx+c)^2 \ln(F))^{47} / 2 e^{b(dx+c)^2 \ln(F)}}{114725174870075432759971875} - \frac{131072 (-b(dx+c)^2 \ln(F))^{45} / 2 e^{b(dx+c)^2 \ln(F)}}{2440961167448413462978125} \\ - \frac{65536 (-b(dx+c)^2 \ln(F))^{43} / 2 e^{b(dx+c)^2 \ln(F)}}{54243581498853632510625} - \frac{32768 (-b(dx+c)^2 \ln(F))^{41} / 2 e^{b(dx+c)^2 \ln(F)}}{1261478639508224011875} \\ - \frac{16384 (-b(dx+c)^2 \ln(F))^{39} / 2 e^{b(dx+c)^2 \ln(F)}}{30767771695322536875} - \frac{8192 (-b(dx+c)^2 \ln(F))^{37} / 2 e^{b(dx+c)^2 \ln(F)}}{788917222956988125} - \frac{4096 (-b(dx+c)^2 \ln(F))^{35} / 2 e^{b(dx+c)^2 \ln(F)}}{21322087106945625} \\ \left. \left. - \frac{2048 (-b(dx+c)^2 \ln(F))^{33} / 2 e^{b(dx+c)^2 \ln(F)}}{609202488769875} - \frac{1024 (-b(dx+c)^2 \ln(F))^{31} / 2 e^{b(dx+c)^2 \ln(F)}}{18460681477875} - \frac{512 (-b(dx+c)^2 \ln(F))^{29} / 2 e^{b(dx+c)^2 \ln(F)}}{595505854125} \right)$$

$$\begin{aligned}
& - \frac{256 (-b (dx + c)^2 \ln(F))^{27/2} e^{b(dx+c)^2 \ln(F)}}{20534684625} - \frac{128 (-b (dx + c)^2 \ln(F))^{25/2} e^{b(dx+c)^2 \ln(F)}}{760543875} - \frac{64 (-b (dx + c)^2 \ln(F))^{23/2} e^{b(dx+c)^2 \ln(F)}}{30421755} \\
& - \frac{32 (-b (dx + c)^2 \ln(F))^{21/2} e^{b(dx+c)^2 \ln(F)}}{1322685} - \frac{16 (-b (dx + c)^2 \ln(F))^{19/2} e^{b(dx+c)^2 \ln(F)}}{62985} - \frac{8 (-b (dx + c)^2 \ln(F))^{17/2} e^{b(dx+c)^2 \ln(F)}}{3315} \\
& - \left. \left. \frac{4 (-b (dx + c)^2 \ln(F))^{15/2} e^{b(dx+c)^2 \ln(F)}}{195} - \frac{2 (-b (dx + c)^2 \ln(F))^{13/2} e^{b(dx+c)^2 \ln(F)}}{13} \right) \right)
\end{aligned}$$

Result (type 4, 1685 leaves):

$$\begin{aligned}
& - \frac{11 d^8 x^9 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 \ln(F)^2 b^2} - \frac{693 d^4 x^5 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{16 \ln(F)^4 b^4} + \frac{3465 d^2 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{32 \ln(F)^5 b^5} + \frac{99 d^6 x^7 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} \\
& + \frac{d^{10} x^{11} F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} - \frac{10395 c F^b d^2 x^2 + 2 b c d x + b c^2 + a}{64 d \ln(F)^6 b^6} - \frac{693 c^5 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{16 d \ln(F)^4 b^4} + \frac{c^{11} F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d \ln(F) b} \\
& - \frac{11 c^9 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 d \ln(F)^2 b^2} + \frac{99 c^7 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 d \ln(F)^3 b^3} + \frac{3465 c^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{32 d \ln(F)^5 b^5} + \frac{693 c^6 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} \\
& - \frac{3465 c^4 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{16 \ln(F)^4 b^4} + \frac{11 c^{10} x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} - \frac{99 c^8 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 \ln(F)^2 b^2} + \frac{10395 c^2 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{32 \ln(F)^5 b^5} \\
& - \frac{10395 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{64 \ln(F)^6 b^6} + \frac{231 d^5 c^5 x^6 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b} + \frac{231 d^4 c^6 x^5 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b} + \frac{165 d^3 c^7 x^4 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b} \\
& + \frac{165 d^2 c^8 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} + \frac{55 d c^9 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} - \frac{99 d c^7 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F)^2 b^2} + \frac{11 d^9 c x^{10} F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} \\
& - \frac{99 d^7 c x^8 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 \ln(F)^2 b^2} - \frac{3465 d^3 c x^4 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{16 \ln(F)^4 b^4} + \frac{10395 d c x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{32 \ln(F)^5 b^5} + \frac{693 d^5 c x^6 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} \\
& + \frac{55 d^8 c^2 x^9 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} + \frac{2079 d^4 c^2 x^5 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} - \frac{3465 d^2 c^2 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^4 b^4} \\
& - \frac{99 d^6 c^2 x^7 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F)^2 b^2} + \frac{165 d^7 c^3 x^8 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b} + \frac{3465 d^3 c^3 x^4 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} \\
& - \frac{3465 d c^3 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^4 b^4} - \frac{231 d^5 c^3 x^6 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F)^2 b^2} - \frac{231 d^2 c^6 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F)^2 b^2} \\
& - \frac{693 d^4 c^4 x^5 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F)^2 b^2} + \frac{3465 d^2 c^4 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} + \frac{165 d^6 c^4 x^7 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b} \\
& - \frac{693 d^3 c^5 x^4 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F)^2 b^2} + \frac{2079 d c^5 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{8 \ln(F)^3 b^3} - \frac{10395 \sqrt{\pi} F^a \operatorname{erf} \left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}} \right)}{128 d \ln(F)^6 b^6 \sqrt{-b \ln(F)}}
\end{aligned}$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^3} (dx+c)^{17} dx$$

Optimal (type 3, 103 leaves, 1 step):

$$\frac{F^{a+b(dx+c)^3} (120 - 120b(dx+c)^3 \ln(F) + 60b^2(dx+c)^6 \ln(F)^2 - 20b^3(dx+c)^9 \ln(F)^3 + 5b^4(dx+c)^{12} \ln(F)^4 - b^5(dx+c)^{15} \ln(F)^5)}{3b^6 d \ln(F)^6}$$

Result (type 3, 856 leaves):

$$\frac{1}{3 \ln(F)^6 b^6 d} \left((-120 + 120 \ln(F) b c^3 - 5 \ln(F)^4 b^4 c^{12} + \ln(F)^5 b^5 c^{15} + 20 \ln(F)^3 b^3 c^9 - 60 \ln(F)^2 b^2 c^6 + 120 d^3 x^3 b \ln(F) - 60 c d^{11} x^{11} \ln(F)^4 b^4 \right. \\ + 3003 \ln(F)^5 b^5 c^{10} d^5 x^5 - 330 c^2 d^{10} x^{10} \ln(F)^4 b^4 + 1365 \ln(F)^5 b^5 c^{11} d^4 x^4 - 1100 \ln(F)^4 b^4 c^3 d^9 x^9 + 455 \ln(F)^5 b^5 c^{12} d^3 x^3 - 2475 \ln(F)^4 b^4 c^4 d^8 x^8 \\ + 105 \ln(F)^5 b^5 c^{13} d^2 x^2 - 3960 \ln(F)^4 b^4 c^5 d^7 x^7 + 15 \ln(F)^5 b^5 c^{14} dx - 4620 \ln(F)^4 b^4 c^6 d^6 x^6 - 3960 \ln(F)^4 b^4 c^7 d^5 x^5 - 2475 \ln(F)^4 b^4 c^8 d^4 x^4 \\ - 1100 \ln(F)^4 b^4 c^9 d^3 x^3 + 180 c d^8 x^8 \ln(F)^3 b^3 - 330 \ln(F)^4 b^4 c^{10} d^2 x^2 + 720 c^2 d^7 x^7 \ln(F)^3 b^3 - 60 \ln(F)^4 b^4 c^{11} dx + 1680 \ln(F)^3 b^3 c^3 d^6 x^6 \\ + 2520 \ln(F)^3 b^3 c^4 d^5 x^5 + 2520 \ln(F)^3 b^3 c^5 d^4 x^4 + 1680 \ln(F)^3 b^3 c^6 d^3 x^3 + 720 \ln(F)^3 b^3 c^7 d^2 x^2 + 180 \ln(F)^3 b^3 c^8 dx - 360 c d^5 x^5 \ln(F)^2 b^2 \\ - 900 \ln(F)^2 b^2 c^2 d^4 x^4 - 1200 \ln(F)^2 b^2 c^3 d^3 x^3 - 900 \ln(F)^2 b^2 c^4 d^2 x^2 - 360 \ln(F)^2 b^2 c^5 dx + 15 d^{14} c x^{14} \ln(F)^5 b^5 + 105 d^{13} c^2 x^{13} \ln(F)^5 b^5 \\ + 455 \ln(F)^5 b^5 c^3 d^{12} x^{12} + 1365 \ln(F)^5 b^5 c^4 d^{11} x^{11} + 3003 \ln(F)^5 b^5 c^5 d^{10} x^{10} + 5005 \ln(F)^5 b^5 c^6 d^9 x^9 + 6435 \ln(F)^5 b^5 c^7 d^8 x^8 + 6435 \ln(F)^5 b^5 c^8 d^7 x^7 \\ + 5005 \ln(F)^5 b^5 c^9 d^6 x^6 + d^{15} x^{15} \ln(F)^5 b^5 - 5 d^{12} x^{12} \ln(F)^4 b^4 + 20 d^9 x^9 \ln(F)^3 b^3 - 60 d^6 x^6 \ln(F)^2 b^2 + 360 \ln(F) b c d^2 x^2 + 360 \ln(F) b c^2 dx \\ \left. F^b d^3 x^3 + 3 b c d^2 x^2 + 3 b c^2 dx + b c^3 + a \right)$$

Problem 76: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^3} (dx+c)^{14} dx$$

Optimal (type 3, 86 leaves, 1 step):

$$\frac{F^{a+b(dx+c)^3} (24 - 24b(dx+c)^3 \ln(F) + 12b^2(dx+c)^6 \ln(F)^2 - 4b^3(dx+c)^9 \ln(F)^3 + b^4(dx+c)^{12} \ln(F)^4)}{3b^5 d \ln(F)^5}$$

Result (type 3, 583 leaves):

$$\frac{1}{3 \ln(F)^5 b^5 d} \left((24 - 24 \ln(F) b c^3 + \ln(F)^4 b^4 c^{12} - 4 \ln(F)^3 b^3 c^9 + 12 \ln(F)^2 b^2 c^6 - 24 d^3 x^3 b \ln(F) + 12 c d^{11} x^{11} \ln(F)^4 b^4 + 66 c^2 d^{10} x^{10} \ln(F)^4 b^4 \right. \\ + 220 \ln(F)^4 b^4 c^3 d^9 x^9 + 495 \ln(F)^4 b^4 c^4 d^8 x^8 + 792 \ln(F)^4 b^4 c^5 d^7 x^7 + 924 \ln(F)^4 b^4 c^6 d^6 x^6 + 792 \ln(F)^4 b^4 c^7 d^5 x^5 + 495 \ln(F)^4 b^4 c^8 d^4 x^4 \\ + 220 \ln(F)^4 b^4 c^9 d^3 x^3 - 36 c d^8 x^8 \ln(F)^3 b^3 + 66 \ln(F)^4 b^4 c^{10} d^2 x^2 - 144 c^2 d^7 x^7 \ln(F)^3 b^3 + 12 \ln(F)^4 b^4 c^{11} dx - 336 \ln(F)^3 b^3 c^3 d^6 x^6 \\ - 504 \ln(F)^3 b^3 c^4 d^5 x^5 - 504 \ln(F)^3 b^3 c^5 d^4 x^4 - 336 \ln(F)^3 b^3 c^6 d^3 x^3 - 144 \ln(F)^3 b^3 c^7 d^2 x^2 - 36 \ln(F)^3 b^3 c^8 dx + 72 c d^5 x^5 \ln(F)^2 b^2 \\ + 180 \ln(F)^2 b^2 c^2 d^4 x^4 + 240 \ln(F)^2 b^2 c^3 d^3 x^3 + 180 \ln(F)^2 b^2 c^4 d^2 x^2 + 72 \ln(F)^2 b^2 c^5 dx + d^{12} x^{12} \ln(F)^4 b^4 - 4 d^9 x^9 \ln(F)^3 b^3 + 12 d^6 x^6 \ln(F)^2 b^2 \\ \left. - 72 \ln(F) b c d^2 x^2 - 72 \ln(F) b c^2 dx \right) F^b d^3 x^3 + 3 b c d^2 x^2 + 3 b c^2 dx + b c^3 + a$$

Problem 77: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^3} (dx+c)^8 dx$$

Optimal(type 3, 90 leaves, 3 steps):

$$\frac{2 F^{a+b(dx+c)^3}}{3 b^3 d \ln(F)^3} - \frac{2 F^{a+b(dx+c)^3} (dx+c)^3}{3 b^2 d \ln(F)^2} + \frac{F^{a+b(dx+c)^3} (dx+c)^6}{3 b d \ln(F)}$$

Result(type 3, 199 leaves):

$$\frac{1}{3 \ln(F)^3 b^3 d} \left((d^6 x^6 \ln(F)^2 b^2 + 6 c d^5 x^5 \ln(F)^2 b^2 + 15 \ln(F)^2 b^2 c^2 d^4 x^4 + 20 \ln(F)^2 b^2 c^3 d^3 x^3 + 15 \ln(F)^2 b^2 c^4 d^2 x^2 + 6 \ln(F)^2 b^2 c^5 dx + \ln(F)^2 b^2 c^6 - 2 d^3 x^3 b \ln(F) - 6 \ln(F) b c d^2 x^2 - 6 \ln(F) b c^2 dx - 2 \ln(F) b c^3 + 2) F^{b d^3 x^3 + 3 b c d^2 x^2 + 3 b c^2 dx + b c^3 + a} \right)$$

Problem 78: Unable to integrate problem.

$$\int \frac{F^{a+b(dx+c)^3}}{(dx+c)^7} dx$$

Optimal(type 4, 81 leaves, 3 steps):

$$-\frac{F^{a+b(dx+c)^3}}{6 d (dx+c)^6} - \frac{b F^{a+b(dx+c)^3} \ln(F)}{6 d (dx+c)^3} + \frac{b^2 F^a \text{Ei}(b(dx+c)^3 \ln(F)) \ln(F)^2}{6 d}$$

Result(type 8, 23 leaves):

$$\int \frac{F^{a+b(dx+c)^3}}{(dx+c)^7} dx$$

Problem 79: Unable to integrate problem.

$$\int F^{a+b(dx+c)^3} dx$$

Optimal(type 4, 41 leaves, 1 step):

$$-\frac{F^a (dx+c) \Gamma\left(\frac{1}{3}, -b(dx+c)^3 \ln(F)\right)}{3 d (-b(dx+c)^3 \ln(F))^{1/3}}$$

Result(type 8, 15 leaves):

$$\int F^{a+b(dx+c)^3} dx$$

Problem 80: Unable to integrate problem.

$$\int F^{a+b\sqrt{dx+c}} dx$$

Optimal(type 3, 58 leaves, 3 steps):

$$-\frac{2f^{a+b\sqrt{dx+c}}}{b^2 d \ln(f)^2} + \frac{2f^{a+b\sqrt{dx+c}} \sqrt{dx+c}}{b d \ln(f)}$$

Result(type 8, 15 leaves):

$$\int f^{a+b\sqrt{dx+c}} dx$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{dx+c}} (dx+c)^4 dx$$

Optimal(type 4, 28 leaves, 1 step):

$$\frac{F^a (dx+c)^5 \text{Ei}_6\left(-\frac{b \ln(F)}{dx+c}\right)}{d}$$

Result(type 4, 633 leaves):

$$\begin{aligned} & \frac{d^4 F^{\frac{xad+ac+b}{dx+c}} x^5}{5} + d^3 F^{\frac{xad+ac+b}{dx+c}} c x^4 + 2 d^2 F^{\frac{xad+ac+b}{dx+c}} c^2 x^3 + 2 d F^{\frac{xad+ac+b}{dx+c}} c^3 x^2 + F^{\frac{xad+ac+b}{dx+c}} c^4 x + \frac{F^{\frac{xad+ac+b}{dx+c}} c^5}{5 d} \\ & + \frac{d^3 b \ln(F) F^{\frac{xad+ac+b}{dx+c}} x^4}{20} + \frac{d^2 b \ln(F) F^{\frac{xad+ac+b}{dx+c}} c x^3}{5} + \frac{3 d b \ln(F) F^{\frac{xad+ac+b}{dx+c}} c^2 x^2}{10} + \frac{b \ln(F) F^{\frac{xad+ac+b}{dx+c}} c^3 x}{5} + \frac{b \ln(F) F^{\frac{xad+ac+b}{dx+c}} c^4}{20 d} \\ & + \frac{d^2 b^2 \ln(F)^2 F^{\frac{xad+ac+b}{dx+c}} x^3}{60} + \frac{d b^2 \ln(F)^2 F^{\frac{xad+ac+b}{dx+c}} c x^2}{20} + \frac{b^2 \ln(F)^2 F^{\frac{xad+ac+b}{dx+c}} c^2 x}{20} + \frac{b^2 \ln(F)^2 F^{\frac{xad+ac+b}{dx+c}} c^3}{60 d} \\ & + \frac{d b^3 \ln(F)^3 F^{\frac{xad+ac+b}{dx+c}} x^2}{120} + \frac{b^3 \ln(F)^3 F^{\frac{xad+ac+b}{dx+c}} c x}{60} + \frac{b^3 \ln(F)^3 F^{\frac{xad+ac+b}{dx+c}} c^2}{120 d} + \frac{b^4 \ln(F)^4 F^{\frac{xad+ac+b}{dx+c}} x}{120} + \frac{b^4 \ln(F)^4 F^{\frac{xad+ac+b}{dx+c}} c}{120 d} \\ & + \frac{b^5 \ln(F)^5 F^a \text{Ei}_1\left(-\frac{b \ln(F)}{dx+c}\right)}{120 d} \end{aligned}$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+\frac{b}{dx+c}}}{(dx+c)^6} dx$$

Optimal(type 3, 92 leaves, 1 step):

$$\frac{F^{a + \frac{b}{dx+c}} (24 (dx+c)^4 - 24 b (dx+c)^3 \ln(F) + 12 b^2 (dx+c)^2 \ln(F)^2 - 4 b^3 (dx+c) \ln(F)^3 + b^4 \ln(F)^4)}{b^5 d (dx+c)^4 \ln(F)^5}$$

Result (type 3, 328 leaves):

$$\frac{1}{(dx+c)^5} \left(-\frac{24 d^4 x^5 e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{b^5 \ln(F)^5} - \frac{(b^4 \ln(F)^4 - 8 \ln(F)^3 b^3 c + 36 \ln(F)^2 b^2 c^2 - 96 \ln(F) b c^3 + 120 c^4) x e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{\ln(F)^5 b^5} \right. \\ \left. + \frac{4 d (\ln(F)^3 b^3 - 9 \ln(F)^2 b^2 c + 36 \ln(F) b c^2 - 60 c^3) x^2 e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{b^5 \ln(F)^5} - \frac{12 d^2 (\ln(F)^2 b^2 - 8 b c \ln(F) + 20 c^2) x^3 e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{b^5 \ln(F)^5} \right. \\ \left. + \frac{24 d^3 (b \ln(F) - 5 c) x^4 e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{b^5 \ln(F)^5} - \frac{(b^4 \ln(F)^4 - 4 \ln(F)^3 b^3 c + 12 \ln(F)^2 b^2 c^2 - 24 \ln(F) b c^3 + 24 c^4) c e^{\left(a + \frac{b}{dx+c}\right) \ln(F)}}{\ln(F)^5 b^5 d} \right)$$

Problem 84: Result more than twice size of optimal antiderivative.

$$\int F^{a + \frac{b}{(dx+c)^2}} (dx+c)^7 dx$$

Optimal (type 4, 29 leaves, 1 step):

$$\frac{F^a (dx+c)^8 \text{Ei}_5\left(-\frac{b \ln(F)}{(dx+c)^2}\right)}{2d}$$

Result (type 4, 645 leaves):

$$\frac{F^a d^7 F^{\frac{b}{(dx+c)^2}} x^8}{8} + \frac{F^a F^{\frac{b}{(dx+c)^2}} c^8}{8d} + F^a F^{\frac{b}{(dx+c)^2}} c^7 x + F^a d^6 F^{\frac{b}{(dx+c)^2}} c x^7 + \frac{7 F^a d^5 F^{\frac{b}{(dx+c)^2}} c^2 x^6}{2} + 7 F^a d^4 F^{\frac{b}{(dx+c)^2}} c^3 x^5 + \frac{35 F^a d^3 F^{\frac{b}{(dx+c)^2}} c^4 x^4}{4} \\ + 7 F^a d^2 F^{\frac{b}{(dx+c)^2}} c^5 x^3 + \frac{7 F^a d F^{\frac{b}{(dx+c)^2}} c^6 x^2}{2} + \frac{F^a b^4 \ln(F)^4 \text{Ei}_1\left(-\frac{b \ln(F)}{(dx+c)^2}\right)}{48d} + \frac{F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^6}{24d} + \frac{F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^4}{48d} \\ + \frac{F^a b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c^2}{48d} + \frac{F^a d^5 b \ln(F) F^{\frac{b}{(dx+c)^2}} x^6}{24} + \frac{F^a d^3 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} x^4}{48} + \frac{F^a d b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} x^2}{48} + \frac{F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^5 x}{4} \\ + \frac{F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^3 x}{12} + \frac{F^a b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c x}{24} + \frac{F^a d^4 b \ln(F) F^{\frac{b}{(dx+c)^2}} c x^5}{4} + \frac{5 F^a d^3 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^2 x^4}{8} \\ + \frac{5 F^a d^2 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^3 x^3}{6} + \frac{5 F^a d b \ln(F) F^{\frac{b}{(dx+c)^2}} c^4 x^2}{8} + \frac{F^a d^2 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c x^3}{12} + \frac{F^a d b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^2 x^2}{8}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int F^{a + \frac{b}{(dx+c)^2}} (dx+c)^{10} dx$$

Optimal (type 4, 218 leaves, 1 step):

$$\frac{1}{2d} \left(F^a (dx+c)^{11} \left[\frac{64\sqrt{\pi} \operatorname{erfc}\left(\sqrt{-\frac{b \ln(F)}{(dx+c)^2}}\right)}{10395} - \frac{64 e^{\frac{b \ln(F)}{(dx+c)^2}}}{10395 \sqrt{-\frac{b \ln(F)}{(dx+c)^2}}} + \frac{32 e^{\frac{b \ln(F)}{(dx+c)^2}}}{10395 \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{3/2}} - \frac{16 e^{\frac{b \ln(F)}{(dx+c)^2}}}{3465 \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{5/2}} \right. \right. \\ \left. \left. + \frac{8 e^{\frac{b \ln(F)}{(dx+c)^2}}}{693 \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{7/2}} - \frac{4 e^{\frac{b \ln(F)}{(dx+c)^2}}}{99 \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{9/2}} + \frac{2 e^{\frac{b \ln(F)}{(dx+c)^2}}}{11 \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{11/2}} \right] \left(-\frac{b \ln(F)}{(dx+c)^2}\right)^{11/2} \right)$$

Result (type 4, 1172 leaves):

$$\frac{2F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^8 x}{11} + \frac{2F^a d^8 b \ln(F) F^{\frac{b}{(dx+c)^2}} x^9}{99} + \frac{4F^a d^6 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} x^7}{693} + \frac{8F^a d^4 b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} x^5}{3465} \\ + \frac{16F^a d^2 b^4 \ln(F)^4 F^{\frac{b}{(dx+c)^2}} x^3}{10395} + \frac{2F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^9}{99d} + \frac{4F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^7}{693d} + \frac{8F^a b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c^5}{3465d} \\ + \frac{16F^a b^4 \ln(F)^4 F^{\frac{b}{(dx+c)^2}} c^3}{10395d} + \frac{32F^a b^5 \ln(F)^5 F^{\frac{b}{(dx+c)^2}} c}{10395d} + \frac{16F^a b^4 \ln(F)^4 F^{\frac{b}{(dx+c)^2}} c^2 x}{3465} + \frac{4F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^6 x}{99} \\ + \frac{8F^a b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c^4 x}{693} + \frac{8F^a d^6 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^2 x^7}{11} + \frac{56F^a d^5 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^3 x^6}{33} + \frac{28F^a d^4 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^4 x^5}{11} \\ + \frac{28F^a d^3 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^5 x^4}{11} + \frac{56F^a d^2 b \ln(F) F^{\frac{b}{(dx+c)^2}} c^6 x^3}{33} + \frac{8F^a d b \ln(F) F^{\frac{b}{(dx+c)^2}} c^7 x^2}{11} + \frac{4F^a d^5 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c x^6}{99} \\ + \frac{4F^a d^4 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^2 x^5}{33} + \frac{20F^a d^3 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^3 x^4}{99} + \frac{20F^a d^2 b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^4 x^3}{99} + \frac{4F^a d b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c^5 x^2}{33} \\ + \frac{8F^a d^3 b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c x^4}{693} + \frac{16F^a d^2 b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c^2 x^3}{693} + \frac{16F^a d b^3 \ln(F)^3 F^{\frac{b}{(dx+c)^2}} c^3 x^2}{693} + \frac{16F^a d b^4 \ln(F)^4 F^{\frac{b}{(dx+c)^2}} c x^2}{3465} \\ + \frac{2F^a d^7 b \ln(F) F^{\frac{b}{(dx+c)^2}} c x^8}{11} - \frac{32F^a b^6 \ln(F)^6 \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt{-b \ln(F)}}{dx+c}\right)}{10395 d \sqrt{-b \ln(F)}} + \frac{32F^a b^5 \ln(F)^5 F^{\frac{b}{(dx+c)^2}} x}{10395} + F^a d^9 F^{\frac{b}{(dx+c)^2}} c x^{10} + 5F^a d^8 F^{\frac{b}{(dx+c)^2}} c^2 x^9$$

$$\begin{aligned}
& + 15 F^a d^7 F^{\frac{b}{(dx+c)^2}} c^3 x^8 + 30 F^a d^6 F^{\frac{b}{(dx+c)^2}} c^4 x^7 + 42 F^a d^5 F^{\frac{b}{(dx+c)^2}} c^5 x^6 + 42 F^a d^4 F^{\frac{b}{(dx+c)^2}} c^6 x^5 + 30 F^a d^3 F^{\frac{b}{(dx+c)^2}} c^7 x^4 + 15 F^a d^2 F^{\frac{b}{(dx+c)^2}} c^8 x^3 \\
& + 5 F^a d F^{\frac{b}{(dx+c)^2}} c^9 x^2 + F^a F^{\frac{b}{(dx+c)^2}} c^{10} x + \frac{F^a d^{10} F^{\frac{b}{(dx+c)^2}} x^{11}}{11} + \frac{F^a F^{\frac{b}{(dx+c)^2}} c^{11}}{11 d}
\end{aligned}$$

Problem 86: Result more than twice size of optimal antiderivative.

$$\int F^{a + \frac{b}{(dx+c)^2}} (dx+c)^4 dx$$

Optimal (type 4, 118 leaves, 5 steps):

$$\frac{F^{a + \frac{b}{(dx+c)^2}} (dx+c)^5}{5 d} + \frac{2 b F^{a + \frac{b}{(dx+c)^2}} (dx+c)^3 \ln(F)}{15 d} + \frac{4 b^2 F^{a + \frac{b}{(dx+c)^2}} (dx+c) \ln(F)^2}{15 d} - \frac{4 b^5 / 2 F^a \operatorname{erfi}\left(\frac{\sqrt{b} \sqrt{\ln(F)}}{dx+c}\right) \ln(F)^5 / 2 \sqrt{\pi}}{15 d}$$

Result (type 4, 323 leaves):

$$\begin{aligned}
& \frac{F^a d^4 F^{\frac{b}{(dx+c)^2}} x^5}{5} + F^a d^3 F^{\frac{b}{(dx+c)^2}} c x^4 + 2 F^a d^2 F^{\frac{b}{(dx+c)^2}} c^2 x^3 + 2 F^a d F^{\frac{b}{(dx+c)^2}} c^3 x^2 + F^a F^{\frac{b}{(dx+c)^2}} c^4 x + \frac{F^a F^{\frac{b}{(dx+c)^2}} c^5}{5 d} \\
& + \frac{2 F^a d^2 b \ln(F) F^{\frac{b}{(dx+c)^2}} x^3}{15} + \frac{2 F^a d b \ln(F) F^{\frac{b}{(dx+c)^2}} c x^2}{5} + \frac{2 F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^2 x}{5} + \frac{2 F^a b \ln(F) F^{\frac{b}{(dx+c)^2}} c^3}{15 d} + \frac{4 F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} x}{15} \\
& + \frac{4 F^a b^2 \ln(F)^2 F^{\frac{b}{(dx+c)^2}} c}{15 d} - \frac{4 F^a b^3 \ln(F)^3 \sqrt{\pi} \operatorname{erf}\left(\frac{\sqrt{-b \ln(F)}}{dx+c}\right)}{15 d \sqrt{-b \ln(F)}}
\end{aligned}$$

Problem 92: Unable to integrate problem.

$$\int F^{a + \frac{b}{(dx+c)^3}} (dx+c)^8 dx$$

Optimal (type 4, 113 leaves, 4 steps):

$$\frac{F^{a + \frac{b}{(dx+c)^3}} (dx+c)^9}{9 d} + \frac{b F^{a + \frac{b}{(dx+c)^3}} (dx+c)^6 \ln(F)}{18 d} + \frac{b^2 F^{a + \frac{b}{(dx+c)^3}} (dx+c)^3 \ln(F)^2}{18 d} - \frac{b^3 F^a \operatorname{Ei}\left(\frac{b \ln(F)}{(dx+c)^3}\right) \ln(F)^3}{18 d}$$

Result (type 8, 23 leaves):

$$\int F^{a + \frac{b}{(dx+c)^3}} (dx+c)^8 dx$$

Problem 93: Unable to integrate problem.

$$\int F^{\frac{a + \frac{b}{(dx+c)^3}}{(dx+c)^2} dx$$

Optimal(type 4, 49 leaves, 2 steps):

$$\frac{F^{\frac{a + \frac{b}{(dx+c)^3}}{(dx+c)^3}}{3d} - \frac{b F^a \operatorname{Ei}\left(\frac{b \ln(F)}{(dx+c)^3}\right) \ln(F)}{3d}$$

Result(type 8, 23 leaves):

$$\int F^{\frac{a + \frac{b}{(dx+c)^3}}{(dx+c)^2} dx$$

Problem 95: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{\frac{a + \frac{b}{(dx+c)^3}}{(dx+c)^7}} dx$$

Optimal(type 3, 58 leaves, 2 steps):

$$\frac{F^{\frac{a + \frac{b}{(dx+c)^3}}{3b^2 d \ln(F)^2}} - \frac{F^{\frac{a + \frac{b}{(dx+c)^3}}{3b d (dx+c)^3 \ln(F)}}$$

Result(type 3, 260 leaves):

$$\begin{aligned} & \frac{1}{(dx+c)^6} \left(\frac{d^5 x^6 e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{3 \ln(F)^2 b^2} - \frac{c^2 (-2c^3 + b \ln(F)) x e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{\ln(F)^2 b^2} - \frac{c^3 (-c^3 + b \ln(F)) e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{3 \ln(F)^2 b^2 d} \right. \\ & - \frac{d^2 (-20c^3 + b \ln(F)) x^3 e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{3 \ln(F)^2 b^2} + \frac{5d^3 c^2 x^4 e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{\ln(F)^2 b^2} + \frac{2d^4 c x^5 e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{\ln(F)^2 b^2} \\ & \left. - \frac{cd (-5c^3 + b \ln(F)) x^2 e^{\left(\frac{a + \frac{b}{(dx+c)^3}\right) \ln(F)}}{\ln(F)^2 b^2} \right) \end{aligned}$$

Problem 96: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{\frac{a + \frac{b}{(dx+c)^3}}{(dx+c)^{10}}} dx$$

Optimal(type 3, 90 leaves, 3 steps):

$$-\frac{2F^{a+\frac{b}{(dx+c)^3}}}{3b^3d\ln(F)^3} + \frac{2F^{a+\frac{b}{(dx+c)^3}}}{3b^2d(dx+c)^3\ln(F)^2} - \frac{F^{a+\frac{b}{(dx+c)^3}}}{3bd(dx+c)^6\ln(F)}$$

Result(type 3, 433 leaves):

$$\begin{aligned} & \frac{1}{(dx+c)^9} \left(-\frac{2d^8x^9e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{3\ln(F)^3b^3} - \frac{c^2(6c^6-4\ln(F)bc^3+\ln(F)^2b^2)x^6e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} \right. \\ & - \frac{c^3(2c^6-2\ln(F)bc^3+\ln(F)^2b^2)e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{3\ln(F)^3b^3d} - \frac{d^2(168c^6-40\ln(F)bc^3+\ln(F)^2b^2)x^3e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{3\ln(F)^3b^3} \\ & + \frac{2d^5(-84c^3+b\ln(F))x^6e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{3\ln(F)^3b^3} - \frac{24d^6c^2x^7e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} - \frac{6d^7cx^8e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} \\ & - \frac{cd(24c^6-10\ln(F)bc^3+\ln(F)^2b^2)x^2e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} + \frac{4cd^4(-21c^3+b\ln(F))x^5e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} \\ & \left. + \frac{2c^2d^3(-42c^3+5b\ln(F))x^4e^{\left(a+\frac{b}{(dx+c)^3}\right)\ln(F)}}{\ln(F)^3b^3} \right) \end{aligned}$$

Problem 97: Unable to integrate problem.

$$\int F^{a+\frac{b}{(dx+c)^3}} (dx+c) dx$$

Optimal(type 4, 43 leaves, 1 step):

$$\frac{F^a(dx+c)^2\Gamma\left(-\frac{2}{3}, -\frac{b\ln(F)}{(dx+c)^3}\right)\left(-\frac{b\ln(F)}{(dx+c)^3}\right)^{2/3}}{3d}$$

Result(type 8, 21 leaves):

$$\int F^{a+\frac{b}{(dx+c)^3}} (dx+c) dx$$

Problem 98: Unable to integrate problem.

$$\int F^{a+b(dx+c)^n} dx$$

Optimal(type 4, 50 leaves, 1 step):

$$-\frac{F^a (dx+c) \Gamma\left(\frac{1}{n}, -b(dx+c)^n \ln(F)\right)}{dn(-b(dx+c)^n \ln(F))^{\frac{1}{n}}}$$

Result(type 8, 15 leaves):

$$\int F^{a+b(dx+c)^n} dx$$

Problem 103: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^2} (fx+e)^5 dx$$

Optimal(type 4, 474 leaves, 14 steps):

$$\begin{aligned} & \frac{f^5 F^{a+b(dx+c)^2}}{b^3 d^6 \ln(F)^3} - \frac{5f^3 (-cf+de)^2 F^{a+b(dx+c)^2}}{b^2 d^6 \ln(F)^2} - \frac{15f^4 (-cf+de) F^{a+b(dx+c)^2} (dx+c)}{4b^2 d^6 \ln(F)^2} - \frac{f^5 F^{a+b(dx+c)^2} (dx+c)^2}{b^2 d^6 \ln(F)^2} + \frac{5f(-cf+de)^4 F^{a+b(dx+c)^2}}{2b d^6 \ln(F)} \\ & + \frac{5f^2 (-cf+de)^3 F^{a+b(dx+c)^2} (dx+c)}{b d^6 \ln(F)} + \frac{5f^3 (-cf+de)^2 F^{a+b(dx+c)^2} (dx+c)^2}{b d^6 \ln(F)} + \frac{5f^4 (-cf+de) F^{a+b(dx+c)^2} (dx+c)^3}{2b d^6 \ln(F)} \\ & + \frac{f^5 F^{a+b(dx+c)^2} (dx+c)^4}{2b d^6 \ln(F)} + \frac{15f^4 (-cf+de) F^a \operatorname{erfi}\left((dx+c)\sqrt{b}\sqrt{\ln(F)}\right)\sqrt{\pi}}{8b^{5/2} d^6 \ln(F)^{5/2}} - \frac{5f^2 (-cf+de)^3 F^a \operatorname{erfi}\left((dx+c)\sqrt{b}\sqrt{\ln(F)}\right)\sqrt{\pi}}{2b^3 /2 d^6 \ln(F)^{3/2}} \\ & + \frac{(-cf+de)^5 F^a \operatorname{erfi}\left((dx+c)\sqrt{b}\sqrt{\ln(F)}\right)\sqrt{\pi}}{2d^6 \sqrt{b}\sqrt{\ln(F)}} \end{aligned}$$

Result(type 4, 1546 leaves):

$$\begin{aligned} & \frac{f^5 x^4 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 \ln(F) b d^2} + \frac{f^5 c^4 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 d^6 \ln(F) b} - \frac{9f^5 c^2 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{4 d^6 \ln(F)^2 b^2} - \frac{f^5 x^2 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{\ln(F)^2 b^2 d^4} \\ & - \frac{5e^2 f^3 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{\ln(F)^2 b^2 d^4} + \frac{5e^4 f F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 \ln(F) b d^2} + \frac{f^5 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{\ln(F)^3 b^3 d^6} + \frac{5e f^4 x^3 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 \ln(F) b d^2} \\ & - \frac{5e f^4 c^3 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 d^5 \ln(F) b} + \frac{25e f^4 c F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{4 d^5 \ln(F)^2 b^2} - \frac{15e f^4 x F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{4 \ln(F)^2 b^2 d^4} + \frac{5e^2 f^3 x^2 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{\ln(F) b d^2} \\ & + \frac{5e^2 f^3 c^2 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{d^4 \ln(F) b} + \frac{5e^3 f^2 x F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{\ln(F) b d^2} - \frac{5e^3 f^2 c F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{d^3 \ln(F) b} \\ & - \frac{5e^3 f^2 c^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d\sqrt{-b \ln(F)} x + \frac{cb \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^3 \sqrt{-b \ln(F)}} + \frac{5e^4 f c \sqrt{\pi} F^a \operatorname{erf}\left(-d\sqrt{-b \ln(F)} x + \frac{cb \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^2 \sqrt{-b \ln(F)}} - \frac{5e f^4 c x^2 F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 d^3 \ln(F) b} \\ & + \frac{5e f^4 c^2 x F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{2 d^4 \ln(F) b} - \frac{5e f^4 c^4 \sqrt{\pi} F^a \operatorname{erf}\left(-d\sqrt{-b \ln(F)} x + \frac{cb \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^5 \sqrt{-b \ln(F)}} - \frac{5e^2 f^3 c x F^{b d^2 x^2 + 2bc dx + b c^2 + a}}{d^3 \ln(F) b} \end{aligned}$$

$$\begin{aligned}
& + \frac{5 e^2 f^3 c^3 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^4 \sqrt{-b \ln(F)}} - \frac{f^5 c x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^3 \ln(F) b} + \frac{f^5 c^2 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^4 \ln(F) b} \\
& - \frac{f^5 c^3 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^5 \ln(F) b} + \frac{f^5 c^5 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^6 \sqrt{-b \ln(F)}} + \frac{7 f^5 c x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 d^5 \ln(F)^2 b^2} \\
& + \frac{15 e f^4 c^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^5 \ln(F) b \sqrt{-b \ln(F)}} - \frac{15 e^2 f^3 c \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^4 \ln(F) b \sqrt{-b \ln(F)}} \\
& - \frac{5 f^5 c^3 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^6 \ln(F) b \sqrt{-b \ln(F)}} + \frac{15 f^5 c \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{8 d^6 \ln(F)^2 b^2 \sqrt{-b \ln(F)}} \\
& - \frac{15 e f^4 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{8 \ln(F)^2 b^2 d^5 \sqrt{-b \ln(F)}} + \frac{5 e^3 f^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 \ln(F) b d^3 \sqrt{-b \ln(F)}} \\
& - \frac{e^5 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d \sqrt{-b \ln(F)}}
\end{aligned}$$

Problem 104: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(dx+c)^2} (fx+e)^4 dx$$

Optimal (type 4, 349 leaves, 11 steps):

$$\begin{aligned}
& - \frac{2 f^3 (-cf+de) F^{a+b(dx+c)^2}}{b^2 d^5 \ln(F)^2} - \frac{3 f^4 F^{a+b(dx+c)^2} (dx+c)}{4 b^2 d^5 \ln(F)^2} + \frac{2 f (-cf+de)^3 F^{a+b(dx+c)^2}}{b d^5 \ln(F)} + \frac{3 f^2 (-cf+de)^2 F^{a+b(dx+c)^2} (dx+c)}{b d^5 \ln(F)} \\
& + \frac{2 f^3 (-cf+de) F^{a+b(dx+c)^2} (dx+c)^2}{b d^5 \ln(F)} + \frac{f^4 F^{a+b(dx+c)^2} (dx+c)^3}{2 b d^5 \ln(F)} + \frac{3 f^4 F^a \operatorname{erfi}\left((dx+c) \sqrt{b} \sqrt{\ln(F)}\right) \sqrt{\pi}}{8 b^5 / 2 d^5 \ln(F)^5 / 2} \\
& - \frac{3 f^2 (-cf+de)^2 F^a \operatorname{erfi}\left((dx+c) \sqrt{b} \sqrt{\ln(F)}\right) \sqrt{\pi}}{2 b^3 / 2 d^5 \ln(F)^3 / 2} + \frac{(-cf+de)^4 F^a \operatorname{erfi}\left((dx+c) \sqrt{b} \sqrt{\ln(F)}\right) \sqrt{\pi}}{2 d^5 \sqrt{b} \sqrt{\ln(F)}}
\end{aligned}$$

Result (type 4, 997 leaves):

$$- \frac{e^4 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d \sqrt{-b \ln(F)}} + \frac{f^4 x^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 \ln(F) b d^2} - \frac{f^4 c x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^3 \ln(F) b} + \frac{f^4 c^2 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^4 \ln(F) b}$$

$$\begin{aligned}
& - \frac{f^4 c^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{2 d^5 \ln(F) b} - \frac{f^4 c^4 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^5 \sqrt{-b \ln(F)}} + \frac{3 f^4 c^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 d^5 \ln(F) b \sqrt{-b \ln(F)}} \\
& + \frac{5 f^4 c F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 d^5 \ln(F)^2 b^2} - \frac{3 f^4 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{4 \ln(F)^2 b^2 d^4} - \frac{3 f^4 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{8 \ln(F)^2 b^2 d^5 \sqrt{-b \ln(F)}} + \frac{2 e f^3 x^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b d^2} \\
& - \frac{2 e f^3 c x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{d^3 \ln(F) b} + \frac{2 e f^3 c^2 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{d^4 \ln(F) b} + \frac{2 e f^3 c^3 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^4 \sqrt{-b \ln(F)}} \\
& - \frac{3 e f^3 c \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^4 \ln(F) b \sqrt{-b \ln(F)}} - \frac{2 e f^3 F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F)^2 b^2 d^4} + \frac{3 e^2 f^2 x F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b d^2} \\
& - \frac{3 e^2 f^2 c F^b d^2 x^2 + 2 b c d x + b c^2 + a}{d^3 \ln(F) b} - \frac{3 e^2 f^2 c^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^3 \sqrt{-b \ln(F)}} + \frac{3 e^2 f^2 \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{2 \ln(F) b d^3 \sqrt{-b \ln(F)}} \\
& + \frac{2 e^3 f F^b d^2 x^2 + 2 b c d x + b c^2 + a}{\ln(F) b d^2} + \frac{2 e^3 f c \sqrt{\pi} F^a \operatorname{erf}\left(-d \sqrt{-b \ln(F)} x + \frac{c b \ln(F)}{\sqrt{-b \ln(F)}}\right)}{d^2 \sqrt{-b \ln(F)}}
\end{aligned}$$

Problem 107: Unable to integrate problem.

$$\int e^{e(dx+c)^3} (bx+a)^2 dx$$

Optimal(type 4, 111 leaves, 5 steps):

$$\frac{b^2 e^{(dx+c)^3}}{3 d^3 e} - \frac{(-ad+bc)^2 (dx+c) \Gamma\left(\frac{1}{3}, -e(dx+c)^3\right)}{3 d^3 (-e(dx+c)^3)^{1/3}} + \frac{2b(-ad+bc)(dx+c)^2 \Gamma\left(\frac{2}{3}, -e(dx+c)^3\right)}{3 d^3 (-e(dx+c)^3)^{2/3}}$$

Result(type 8, 20 leaves):

$$\int e^{e(dx+c)^3} (bx+a)^2 dx$$

Problem 111: Unable to integrate problem.

$$\int \frac{e}{e^{(dx+c)^3}} (bx+a)^2 dx$$

Optimal(type 4, 134 leaves, 6 steps):

$$\frac{b^2 e^{\frac{e}{(dx+c)^3}} (dx+c)^3}{3 d^3} - \frac{b^2 e \operatorname{Ei}\left(\frac{e}{(dx+c)^3}\right)}{3 d^3} - \frac{2 b (-ad+bc) \left(-\frac{e}{(dx+c)^3}\right)^{2/3} (dx+c)^2 \Gamma\left(-\frac{2}{3}, -\frac{e}{(dx+c)^3}\right)}{3 d^3}$$

$$+ \frac{(-ad+bc)^2 \left(-\frac{e}{(dx+c)^3}\right)^{1/3} (dx+c) \Gamma\left(-\frac{1}{3}, -\frac{e}{(dx+c)^3}\right)}{3 d^3}$$

Result(type 8, 20 leaves):

$$\int e^{\frac{e}{(dx+c)^3}} (bx+a)^2 dx$$

Problem 112: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{e+\frac{f(bx+a)}{dx+c}}}{hx+g} dx$$

Optimal(type 4, 104 leaves, 5 steps):

$$-\frac{F^{e+\frac{bf}{d}} \operatorname{Ei}\left(-\frac{(-ad+bc)f \ln(F)}{d(dx+c)}\right)}{h} + \frac{F^{e+\frac{f(-ah+bg)}{-hc+gd}} \operatorname{Ei}\left(-\frac{(-ad+bc)f(hx+g) \ln(F)}{(-hc+gd)(dx+c)}\right)}{h}$$

Result(type 4, 431 leaves):

$$-\frac{\frac{afh-bfg+ceh-deg}{dF} \operatorname{Ei}_1\left(-\frac{f(ad-bc) \ln(F)}{d(dx+c)} - \frac{(fb+de) \ln(F)}{d} - \frac{-\ln(F)afh + \ln(F)bfg - \ln(F)ceh + \ln(F)deg}{hc-gd}\right) a}{h(ad-bc)}$$

$$+ \frac{\frac{afh-bfg+ceh-deg}{F} \operatorname{Ei}_1\left(-\frac{f(ad-bc) \ln(F)}{d(dx+c)} - \frac{(fb+de) \ln(F)}{d} - \frac{-\ln(F)afh + \ln(F)bfg - \ln(F)ceh + \ln(F)deg}{hc-gd}\right) bc}{h(ad-bc)}$$

$$+ \frac{\frac{fb+de}{dF} \operatorname{Ei}_1\left(-\frac{f(ad-bc) \ln(F)}{d(dx+c)} - \frac{(fb+de) \ln(F)}{d} - \frac{-\ln(F)bf - de \ln(F)}{d}\right) a}{h(ad-bc)}$$

$$- \frac{\frac{fb+de}{F} \operatorname{Ei}_1\left(-\frac{f(ad-bc) \ln(F)}{d(dx+c)} - \frac{(fb+de) \ln(F)}{d} - \frac{-\ln(F)bf - de \ln(F)}{d}\right) bc}{h(ad-bc)}$$

Problem 113: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{+\frac{f(bx+a)}{dx+c}}}{(hx+g)^4} dx$$

Optimal(type 4, 618 leaves, 48 steps):

$$\begin{aligned} & \frac{d^3 F^{e+\frac{bf}{d}-\frac{(-ad+bc)f}{d(dx+c)}}}{3h(-hc+gd)^3} - \frac{F^{e+\frac{f(bx+a)}{dx+c}}}{3h(hx+g)^3} + \frac{5d^2(-ad+bc)fF^{e+\frac{bf}{d}-\frac{(-ad+bc)f}{d(dx+c)}} \ln(F)}{6(-hc+gd)^4} - \frac{(-ad+bc)fF^{e+\frac{f(bx+a)}{dx+c}} \ln(F)}{6(-hc+gd)^2(hx+g)^2} \\ & - \frac{2d(-ad+bc)fF^{e+\frac{f(bx+a)}{dx+c}} \ln(F)}{3(-hc+gd)^3(hx+g)} + \frac{d^2(-ad+bc)fF^{e+\frac{f(-ah+bg)}{-hc+gd}} \operatorname{Ei}\left(-\frac{(-ad+bc)f(hx+g)\ln(F)}{(-hc+gd)(dx+c)}\right) \ln(F)}{(-hc+gd)^4} \\ & + \frac{d(-ad+bc)^2 f^2 F^{e+\frac{bf}{d}-\frac{(-ad+bc)f}{d(dx+c)}} h \ln(F)^2}{6(-hc+gd)^5} - \frac{(-ad+bc)^2 f^2 F^{e+\frac{f(bx+a)}{dx+c}} h \ln(F)^2}{6(-hc+gd)^4(hx+g)} \\ & + \frac{d(-ad+bc)^2 f^2 F^{e+\frac{f(-ah+bg)}{-hc+gd}} h \operatorname{Ei}\left(-\frac{(-ad+bc)f(hx+g)\ln(F)}{(-hc+gd)(dx+c)}\right) \ln(F)^2}{(-hc+gd)^5} \\ & + \frac{(-ad+bc)^3 f^3 F^{e+\frac{f(-ah+bg)}{-hc+gd}} h^2 \operatorname{Ei}\left(-\frac{(-ad+bc)f(hx+g)\ln(F)}{(-hc+gd)(dx+c)}\right) \ln(F)^3}{6(-hc+gd)^6} \end{aligned}$$

Result(type ?, 4470 leaves): Display of huge result suppressed!

Problem 120: Result more than twice size of optimal antiderivative.

$$\int e^{cx^2+bx+a} (ex+d)^3 dx$$

Optimal(type 4, 226 leaves, 10 steps):

$$\begin{aligned} & -\frac{e^3 f e^{cx^2+bx+a}}{2c^2 \ln(f)^2} + \frac{e(-be+2dc)^2 f e^{cx^2+bx+a}}{8c^3 \ln(f)} + \frac{e(-be+2dc) f e^{cx^2+bx+a} (ex+d)}{4c^2 \ln(f)} + \frac{e f e^{cx^2+bx+a} (ex+d)^2}{2c \ln(f)} \\ & - \frac{3e^2(-be+2dc) f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{(2cx+b)\sqrt{\ln(f)}}{2\sqrt{c}}\right) \sqrt{\pi}}{8c^5 / 2 \ln(f)^3 / 2} + \frac{(-be+2dc)^3 f^{a-\frac{b^2}{4c}} \operatorname{erfi}\left(\frac{(2cx+b)\sqrt{\ln(f)}}{2\sqrt{c}}\right) \sqrt{\pi}}{16c^7 / 2 \sqrt{\ln(f)}} \end{aligned}$$

Result(type 4, 552 leaves):

$$-\frac{d^3 \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{2\sqrt{-c \ln(f)}} + \frac{e^3 x^2 f e^{cx^2+bx+a}}{2c \ln(f)} - \frac{e^3 b x f e^{cx^2+bx+a}}{4c^2 \ln(f)} + \frac{e^3 b^2 f e^{cx^2+bx+a}}{8c^3 \ln(f)}$$

$$\begin{aligned}
& + \frac{e^3 b^3 \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{16 c^3 \sqrt{-c \ln(f)}} - \frac{3 e^3 b \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{8 c^2 \ln(f) \sqrt{-c \ln(f)}} - \frac{e^3 f e^{bx+a}}{2 c^2 \ln(f)^2} \\
& + \frac{3 d e^2 x f e^{bx+a}}{2 c \ln(f)} - \frac{3 d e^2 b f e^{bx+a}}{4 c^2 \ln(f)} - \frac{3 d e^2 b^2 \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{8 c^2 \sqrt{-c \ln(f)}} \\
& + \frac{3 d e^2 \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{4 c \ln(f) \sqrt{-c \ln(f)}} + \frac{3 d^2 e f e^{bx+a}}{2 c \ln(f)} + \frac{3 d^2 e b \sqrt{\pi} f^{\frac{4ac-b^2}{4c}} \operatorname{erf}\left(-\sqrt{-c \ln(f)} x + \frac{\ln(f) b}{2\sqrt{-c \ln(f)}}\right)}{4 c \sqrt{-c \ln(f)}}
\end{aligned}$$

Problem 127: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{ex+d}}{x^2 (cx^2 + bx + a)} dx$$

Optimal (type 4, 184 leaves, 9 steps):

$$\begin{aligned}
& - \frac{e^{ex+d}}{ax} - \frac{b e^d \operatorname{Ei}(ex)}{a^2} + \frac{e e^d \operatorname{Ei}(ex)}{a} + \frac{e^{d - \frac{e(b + \sqrt{-4ac + b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b + 2cx + \sqrt{-4ac + b^2})}{2c}\right) \left(b + \frac{2ac - b^2}{\sqrt{-4ac + b^2}}\right)}{2a^2} \\
& + \frac{e^{d - \frac{e(b - \sqrt{-4ac + b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b + 2cx - \sqrt{-4ac + b^2})}{2c}\right) \left(b + \frac{-2ac + b^2}{\sqrt{-4ac + b^2}}\right)}{2a^2}
\end{aligned}$$

Result (type 4, 560 leaves):

$$\begin{aligned}
& e \left(- \frac{e^{ex+d}}{axe} - \frac{(ae - b) e^d \operatorname{Ei}_1(-ex)}{a^2 e} - \frac{1}{2a^2 e \sqrt{-4ace^2 + b^2 e^2}} \left(\right. \right. \\
& - 2e \frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) ace \\
& + e \frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) b^2 e + 2e \frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c} \operatorname{Ei}_1\left(\right. \\
& \left. \left. - \frac{2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c} \right) ace - e \frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c} \operatorname{Ei}_1\left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) b^2 e
\end{aligned}$$

$$+ e^{\frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} b + e^{\frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} b \right)$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{ex+d}}{x(cx^2+bx+a)} dx$$

Optimal (type 4, 142 leaves, 7 steps):

$$\frac{e^d \operatorname{Ei}(ex)}{a} - \frac{e^{\frac{d - \frac{e(b+\sqrt{-4ac+b^2})}{2c}}}}{2a} \operatorname{Ei} \left(\frac{e(b+2cx+\sqrt{-4ac+b^2})}{2c} \right) \left(1 - \frac{b}{\sqrt{-4ac+b^2}} \right) - \frac{e^{\frac{d - \frac{e(b-\sqrt{-4ac+b^2})}{2c}}}}{2a} \operatorname{Ei} \left(\frac{e(b+2cx-\sqrt{-4ac+b^2})}{2c} \right) \left(1 + \frac{b}{\sqrt{-4ac+b^2}} \right)$$

Result (type 4, 368 leaves):

$$-\frac{e^d \operatorname{Ei}_1(-ex)}{a} + \frac{1}{2a\sqrt{-4ace^2+b^2e^2}} \left(e^{\frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) b e - e^{\frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) b e + e^{\frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} + e^{\frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c}} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} \right)$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{ex+d} x^2}{cx^2+bx+a} dx$$

Optimal (type 4, 160 leaves, 7 steps):

$$\frac{e^{ex+d}}{ce} - \frac{e^{d - \frac{e(b - \sqrt{-4ac + b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b + 2cx - \sqrt{-4ac + b^2})}{2c}\right) \left(b + \frac{2ac - b^2}{\sqrt{-4ac + b^2}}\right)}{2c^2}$$

$$- \frac{e^{d - \frac{e(b + \sqrt{-4ac + b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b + 2cx + \sqrt{-4ac + b^2})}{2c}\right) \left(b + \frac{-2ac + b^2}{\sqrt{-4ac + b^2}}\right)}{2c^2}$$

Result (type 4, 1729 leaves):

$$\frac{1}{e^3} \left(\frac{e^2 e^{ex+d}}{c} + \frac{1}{2c^2 \sqrt{-4ace^2 + b^2 e^2}} \left(e^2 \left(2e^{\frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) ace^2 \right. \right. \right.$$

$$\left. - e^{\frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) b^2 e^2 \right.$$

$$\left. + 2e^{\frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) bcde \right.$$

$$\left. - 2e^{\frac{-be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c - be + 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) c^2 d^2 - 2e^{\frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) ace^2 \right.$$

$$\left. + e^{\frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) b^2 e^2 \right.$$

$$\left. - 2e^{\frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) bcde + 2e^{\frac{-be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}} \operatorname{Ei}_1\left(\frac{-2(ex+d)c + be - 2dc + \sqrt{-4ace^2 + b^2 e^2}}{2c}\right) c^2 d^2 \right)$$

$$\begin{aligned}
& + e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} be \\
& - 2e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} cd + e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\right. \\
& \left. - \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} be - 2e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\right. \\
& \left. - \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} cd \left. \right) \\
& - \frac{1}{\sqrt{-4ace^2+b^2e^2}} \left(d^2 e^2 \left(e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) - e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\right. \right. \right. \\
& \left. \left. - \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \right) \right) + \frac{1}{c\sqrt{-4ace^2+b^2e^2}} \left(d e^2 \left(\right. \right. \\
& \left. - e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) be \right. \\
& \left. + 2e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) cd + e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\right. \right. \\
& \left. - \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) be - 2e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(- \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) cd \\
& \left. + e \frac{-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\frac{-2(ex+d)c-be+2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} + e \frac{-be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \operatorname{Ei}_1 \left(\right. \right. \\
& \left. \left. - \frac{2(ex+d)c+be-2dc+\sqrt{-4ace^2+b^2e^2}}{2c} \right) \sqrt{-4ace^2+b^2e^2} \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 130: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{ex+d} x^3}{cx^2 + bx + a} dx$$

Optimal (type 4, 203 leaves, 9 steps):

$$-\frac{e^{ex+d}}{ce^2} - \frac{be^{ex+d}}{c^2e} + \frac{e^{ex+d}x}{ce} + \frac{e^{d-\frac{e(b-\sqrt{-4ac+b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b+2cx-\sqrt{-4ac+b^2})}{2c}\right) \left(b^2 - ac - \frac{b(-3ac+b^2)}{\sqrt{-4ac+b^2}}\right)}{2c^3} + \frac{e^{d-\frac{e(b+\sqrt{-4ac+b^2})}{2c}} \operatorname{Ei}\left(\frac{e(b+2cx+\sqrt{-4ac+b^2})}{2c}\right) \left(b^2 - ac + \frac{b(-3ac+b^2)}{\sqrt{-4ac+b^2}}\right)}{2c^3}$$

Result (type ?, 3531 leaves): Display of huge result suppressed!

Problem 133: Result more than twice size of optimal antiderivative.

$$\int \frac{2^x}{a - 2^{2x}b} dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{\operatorname{arctanh}\left(\frac{2^x\sqrt{b}}{\sqrt{a}}\right)}{\ln(2)\sqrt{a}\sqrt{b}}$$

Result (type 3, 48 leaves):

$$\frac{\ln\left(2^x + \frac{a}{\sqrt{ab}}\right)}{2\sqrt{ab}\ln(2)} - \frac{\ln\left(2^x - \frac{a}{\sqrt{ab}}\right)}{2\sqrt{ab}\ln(2)}$$

Problem 134: Unable to integrate problem.

$$\int \frac{2^x}{\sqrt{a - 4^x b}} dx$$

Optimal (type 3, 26 leaves, 3 steps):

$$\frac{\operatorname{arctan}\left(\frac{2^x\sqrt{b}}{\sqrt{a - 4^x b}}\right)}{\ln(2)\sqrt{b}}$$

Result (type 8, 16 leaves):

$$\int \frac{2^x}{\sqrt{a-4^x b}} dx$$

Problem 141: Result more than twice size of optimal antiderivative.

$$\int \frac{d + e f^{hx+g}}{a + b f^{hx+g} + c f^{2hx+2g}} dx$$

Optimal (type 3, 97 leaves, 7 steps):

$$\frac{dx}{a} - \frac{d \ln(a + b f^{hx+g} + c f^{2hx+2g})}{2 a h \ln(f)} + \frac{(-2 a e + d b) \operatorname{arctanh}\left(\frac{b + 2 c f^{hx+g}}{\sqrt{-4 a c + b^2}}\right)}{a h \ln(f) \sqrt{-4 a c + b^2}}$$

Result (type 3, 992 leaves):

$$\begin{aligned} & \frac{4 \ln(f)^2 a c d h^2 x}{4 \ln(f)^2 a^2 c h^2 - \ln(f)^2 a b^2 h^2} - \frac{\ln(f)^2 b^2 d h^2 x}{4 \ln(f)^2 a^2 c h^2 - \ln(f)^2 a b^2 h^2} + \frac{4 \ln(f)^2 a c d g h}{4 \ln(f)^2 a^2 c h^2 - \ln(f)^2 a b^2 h^2} - \frac{\ln(f)^2 b^2 d g h}{4 \ln(f)^2 a^2 c h^2 - \ln(f)^2 a b^2 h^2} \\ & - \frac{2 \ln\left(f^{hx+g} + \frac{2 a b e - b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)}\right) c d}{(4 a c - b^2) h \ln(f)} \\ & + \frac{\ln\left(f^{hx+g} + \frac{2 a b e - b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)}\right) b^2 d}{2 a (4 a c - b^2) h \ln(f)} + \frac{1}{2 a (4 a c - b^2) h \ln(f)} \left(\ln\left(f^{hx+g} \right. \right. \\ & \left. \left. + \frac{2 a b e - b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)} \right) \right. \\ & \left. \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2} \right) \\ & - \frac{2 \ln\left(f^{hx+g} - \frac{-2 a b e + b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)}\right) c d}{(4 a c - b^2) h \ln(f)} \\ & + \frac{\ln\left(f^{hx+g} - \frac{-2 a b e + b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)}\right) b^2 d}{2 a (4 a c - b^2) h \ln(f)} \\ & - \frac{1}{2 a (4 a c - b^2) h \ln(f)} \left(\ln\left(f^{hx+g} \right. \right. \\ & \left. \left. - \frac{-2 a b e + b^2 d + \sqrt{-16 a^3 c e^2 + 4 a^2 b^2 e^2 + 16 a^2 b c d e - 4 a b^3 d e - 4 a b^2 c d^2 + b^4 d^2}}{2 c (2 a e - d b)} \right) \right) \end{aligned}$$

$$\sqrt{-16a^3ce^2 + 4a^2b^2e^2 + 16a^2bcde - 4ab^3de - 4ab^2cd^2 + b^4d^2}$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{a + bf^{-dx-c} + cf^{dx+c}} dx$$

Optimal (type 3, 43 leaves, 4 steps):

$$\frac{2 \operatorname{arctanh}\left(\frac{a + 2cf^{dx+c}}{\sqrt{a^2 - 4bc}}\right)}{d \ln(f) \sqrt{a^2 - 4bc}}$$

Result (type 3, 134 leaves):

$$\frac{\ln\left(f^{-dx-c} + \frac{a\sqrt{a^2-4bc} + a^2 - 4bc}{2b\sqrt{a^2-4bc}}\right)}{\sqrt{a^2-4bc} d \ln(f)} - \frac{\ln\left(f^{-dx-c} + \frac{a\sqrt{a^2-4bc} - a^2 + 4bc}{2b\sqrt{a^2-4bc}}\right)}{\sqrt{a^2-4bc} d \ln(f)}$$

Problem 145: Result more than twice size of optimal antiderivative.

$$\int \frac{x}{a + bf^{-dx-c} + cf^{dx+c}} dx$$

Optimal (type 4, 187 leaves, 8 steps):

$$\frac{x \ln\left(1 + \frac{2cf^{dx+c}}{a - \sqrt{a^2-4bc}}\right)}{d \ln(f) \sqrt{a^2-4bc}} - \frac{x \ln\left(1 + \frac{2cf^{dx+c}}{a + \sqrt{a^2-4bc}}\right)}{d \ln(f) \sqrt{a^2-4bc}} + \frac{\operatorname{polylog}\left(2, -\frac{2cf^{dx+c}}{a - \sqrt{a^2-4bc}}\right)}{d^2 \ln(f)^2 \sqrt{a^2-4bc}} - \frac{\operatorname{polylog}\left(2, -\frac{2cf^{dx+c}}{a + \sqrt{a^2-4bc}}\right)}{d^2 \ln(f)^2 \sqrt{a^2-4bc}}$$

Result (type 4, 425 leaves):

$$\frac{\ln\left(\frac{-2bf^{-dx-c} + \sqrt{a^2-4bc} - a}{-a + \sqrt{a^2-4bc}}\right) x}{\ln(f) d \sqrt{a^2-4bc}} + \frac{\ln\left(\frac{2bf^{-dx-c} + \sqrt{a^2-4bc} + a}{a + \sqrt{a^2-4bc}}\right) x}{\ln(f) d \sqrt{a^2-4bc}} - \frac{\ln\left(\frac{-2bf^{-dx-c} + \sqrt{a^2-4bc} - a}{-a + \sqrt{a^2-4bc}}\right) c}{\ln(f) d^2 \sqrt{a^2-4bc}} + \frac{\ln\left(\frac{2bf^{-dx-c} + \sqrt{a^2-4bc} + a}{a + \sqrt{a^2-4bc}}\right) c}{\ln(f) d^2 \sqrt{a^2-4bc}} + \frac{\operatorname{dilog}\left(\frac{-2bf^{-dx-c} + \sqrt{a^2-4bc} - a}{-a + \sqrt{a^2-4bc}}\right)}{\ln(f)^2 d^2 \sqrt{a^2-4bc}} - \frac{\operatorname{dilog}\left(\frac{2bf^{-dx-c} + \sqrt{a^2-4bc} + a}{a + \sqrt{a^2-4bc}}\right)}{\ln(f)^2 d^2 \sqrt{a^2-4bc}}$$

$$+ \frac{2c \arctan\left(\frac{2bf^{-dx-c} + a}{\sqrt{-a^2 + 4bc}}\right)}{\ln(f) d^2 \sqrt{-a^2 + 4bc}}$$

Problem 147: Unable to integrate problem.

$$\int \frac{\frac{c\sqrt{ex+d}}{a + bF\sqrt{-efx+df}}}{-e^2 x^2 + d^2} dx$$

Optimal(type 4, 60 leaves, 4 steps):

$$\frac{b \operatorname{Ei}\left(\frac{c \ln(F) \sqrt{ex+d}}{\sqrt{-efx+df}}\right)}{de} + \frac{a \ln\left(\frac{\sqrt{ex+d}}{\sqrt{-efx+df}}\right)}{de}$$

Result(type 8, 43 leaves):

$$\int \frac{\frac{c\sqrt{ex+d}}{a + bF\sqrt{-efx+df}}}{-e^2 x^2 + d^2} dx$$

Problem 149: Unable to integrate problem.

$$\int \frac{\left(\frac{\sqrt{-ax+1}}{F\sqrt{ax+1}}\right)^n}{-a^2 x^2 + 1} dx$$

Optimal(type 4, 66 leaves, 3 steps):

$$-\frac{\left(\frac{\sqrt{-ax+1}}{F\sqrt{ax+1}}\right)^n \operatorname{Ei}\left(\frac{n \ln(F) \sqrt{-ax+1}}{\sqrt{ax+1}}\right)}{aF \sqrt{ax+1}}$$

Result(type 8, 35 leaves):

$$\int \frac{\left(\frac{\sqrt{-ax+1}}{F\sqrt{ax+1}}\right)^n}{-a^2 x^2 + 1} dx$$

Problem 150: Unable to integrate problem.

$$\int \frac{3\sqrt{-ax+1}}{F\sqrt{ax+1}(-a^2x^2+1)} dx$$

Optimal(type 4, 25 leaves, 2 steps):

$$-\frac{\operatorname{Ei}\left(\frac{3\ln(F)\sqrt{-ax+1}}{\sqrt{ax+1}}\right)}{a}$$

Result(type 8, 34 leaves):

$$\int \frac{3\sqrt{-ax+1}}{F\sqrt{ax+1}(-a^2x^2+1)} dx$$

Problem 151: Unable to integrate problem.

$$\int \frac{\sqrt{-ax+1}}{F\sqrt{ax+1}(-a^2x^2+1)} dx$$

Optimal(type 4, 24 leaves, 2 steps):

$$-\frac{\operatorname{Ei}\left(\frac{\ln(F)\sqrt{-ax+1}}{\sqrt{ax+1}}\right)}{a}$$

Result(type 8, 33 leaves):

$$\int \frac{\sqrt{-ax+1}}{F\sqrt{ax+1}(-a^2x^2+1)} dx$$

Problem 152: Unable to integrate problem.

$$\int \frac{1}{F\sqrt{ax+1}(-a^2x^2+1)} dx$$

Optimal(type 4, 25 leaves, 2 steps):

$$\frac{\operatorname{Ei}\left(-\frac{\ln(F)\sqrt{-ax+1}}{\sqrt{ax+1}}\right)}{a}$$

Result(type 8, 35 leaves):

$$\int \frac{1}{F \sqrt{ax+1} (-a^2x^2+1)} dx$$

Problem 153: Result more than twice size of optimal antiderivative.

$$\int \frac{a^x b^x}{x^2} dx$$

Optimal(type 4, 26 leaves, 3 steps):

$$-\frac{a^x b^x}{x} + \operatorname{Ei}(x(\ln(a) + \ln(b))) (\ln(a) + \ln(b))$$

Result(type 4, 159 leaves):

$$-\ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right) \left(\frac{1}{x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)} + 1 - \ln(x) - \operatorname{I}\pi - \ln(\ln(b)) - \ln\left(1 + \frac{\ln(a)}{\ln(b)}\right) - \frac{2x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right) + 2}{2x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)} + \frac{e^{x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)}}{x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)} \right. \\ \left. + \ln\left(-x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)\right) + \operatorname{Ei}_1\left(-x \ln(b) \left(1 + \frac{\ln(a)}{\ln(b)}\right)\right) \right)$$

Problem 154: Unable to integrate problem.

$$\int \frac{(d + e^{ix+h})(gx+f)^3}{a + b e^{ix+h} + c e^{2ix+2h}} dx$$

Optimal(type 4, 692 leaves, 13 steps):

$$\frac{(gx+f)^4 \left(e + \frac{-be+2dc}{\sqrt{-4ac+b^2}}\right)}{4g(b - \sqrt{-4ac+b^2})} - \frac{(gx+f)^3 \ln\left(1 + \frac{2ce^{ix+h}}{b - \sqrt{-4ac+b^2}}\right) \left(e + \frac{-be+2dc}{\sqrt{-4ac+b^2}}\right)}{i(b - \sqrt{-4ac+b^2})} \\ - \frac{3g(gx+f)^2 \operatorname{polylog}\left(2, -\frac{2ce^{ix+h}}{b - \sqrt{-4ac+b^2}}\right) \left(e + \frac{-be+2dc}{\sqrt{-4ac+b^2}}\right)}{i^2(b - \sqrt{-4ac+b^2})} + \frac{6g^2(gx+f) \operatorname{polylog}\left(3, -\frac{2ce^{ix+h}}{b - \sqrt{-4ac+b^2}}\right) \left(e + \frac{-be+2dc}{\sqrt{-4ac+b^2}}\right)}{i^3(b - \sqrt{-4ac+b^2})}$$

$$\begin{aligned}
& - \frac{6g^3 \operatorname{polylog}\left(4, -\frac{2ce^{ix+h}}{b-\sqrt{-4ac+b^2}}\right) \left(e + \frac{-be+2dc}{\sqrt{-4ac+b^2}}\right)}{i^4 (b-\sqrt{-4ac+b^2})} + \frac{(gx+f)^4 \left(e + \frac{be-2dc}{\sqrt{-4ac+b^2}}\right)}{4g (b+\sqrt{-4ac+b^2})} \\
& - \frac{(gx+f)^3 \ln\left(1 + \frac{2ce^{ix+h}}{b+\sqrt{-4ac+b^2}}\right) \left(e + \frac{be-2dc}{\sqrt{-4ac+b^2}}\right)}{i (b+\sqrt{-4ac+b^2})} - \frac{3g (gx+f)^2 \operatorname{polylog}\left(2, -\frac{2ce^{ix+h}}{b+\sqrt{-4ac+b^2}}\right) \left(e + \frac{be-2dc}{\sqrt{-4ac+b^2}}\right)}{i^2 (b+\sqrt{-4ac+b^2})} \\
& + \frac{6g^2 (gx+f) \operatorname{polylog}\left(3, -\frac{2ce^{ix+h}}{b+\sqrt{-4ac+b^2}}\right) \left(e + \frac{be-2dc}{\sqrt{-4ac+b^2}}\right)}{i^3 (b+\sqrt{-4ac+b^2})} - \frac{6g^3 \operatorname{polylog}\left(4, -\frac{2ce^{ix+h}}{b+\sqrt{-4ac+b^2}}\right) \left(e + \frac{be-2dc}{\sqrt{-4ac+b^2}}\right)}{i^4 (b+\sqrt{-4ac+b^2})}
\end{aligned}$$

Result(type 8, 43 leaves):

$$\int \frac{(d + e^{ix+h}) (gx+f)^3}{a + b e^{ix+h} + c e^{2ix+2h}} dx$$

Problem 155: Unable to integrate problem.

$$\int F^{a+b \ln(c+dx^n)} x^2 dx$$

Optimal(type 5, 66 leaves, 4 steps):

$$\frac{F^a x^3 (c + dx^n)^{b \ln(F)} \operatorname{hypergeom}\left(\left[\frac{3}{n}, -b \ln(F)\right], \left[\frac{3+n}{n}\right], -\frac{dx^n}{c}\right)}{3 \left(1 + \frac{dx^n}{c}\right)^{b \ln(F)}}$$

Result(type 8, 20 leaves):

$$\int F^{a+b \ln(c+dx^n)} x^2 dx$$

Problem 156: Unable to integrate problem.

$$\int F^{f(a+b \ln(c(ex+d)^n)^2)} dx$$

Optimal(type 4, 99 leaves, 3 steps):

$$\frac{F^{af} (ex+d) \operatorname{erfi}\left(\frac{1+2bf n \ln(F) \ln(c(ex+d)^n)}{2n\sqrt{b}\sqrt{f}\sqrt{\ln(F)}}\right) \sqrt{\pi}}{2e e^{4bf n^2 \ln(F)} n (c(ex+d)^n)^{\frac{1}{n}} \sqrt{b}\sqrt{f}\sqrt{\ln(F)}}$$

Result(type 8, 22 leaves):

$$\int F^{f(a+b \ln(c(ex+d)^n)^2)} dx$$

Problem 157: Unable to integrate problem.

$$\int \frac{F^{f(a+b \ln(c(ex+d)^n)^2)}{(egx+gd)^3} dx$$

Optimal(type 4, 102 leaves, 3 steps):

$$-\frac{F^{af}(c(ex+d)^n)^{\frac{2}{n}} \operatorname{erfi}\left(\frac{1-bfn \ln(F) \ln(c(ex+d)^n)}{n\sqrt{b}\sqrt{f}\sqrt{\ln(F)}}\right) \sqrt{\pi}}{2e e^{bf n^2 \ln(F)} g^3 n (ex+d)^2 \sqrt{b}\sqrt{f}\sqrt{\ln(F)}}$$

Result(type 8, 33 leaves):

$$\int \frac{F^{f(a+b \ln(c(ex+d)^n)^2)}{(egx+gd)^3} dx$$

Problem 158: Unable to integrate problem.

$$\int F^{f(a+b \ln(c(ex+d)^n)^2)} dx$$

Optimal(type 4, 99 leaves, 3 steps):

$$\frac{F^{af}(ex+d) \operatorname{erfi}\left(\frac{1+2bfn \ln(F) \ln(c(ex+d)^n)}{2n\sqrt{b}\sqrt{f}\sqrt{\ln(F)}}\right) \sqrt{\pi}}{2e e^{4bf n^2 \ln(F)} n (c(ex+d)^n)^{\frac{1}{n}} \sqrt{b}\sqrt{f}\sqrt{\ln(F)}}$$

Result(type 8, 22 leaves):

$$\int F^{f(a+b \ln(c(ex+d)^n)^2)} dx$$

Problem 160: Unable to integrate problem.

$$\int F^{f(a+b \ln(c(ex+d)^n)^2)} (egx+gd) dx$$

Optimal(type 4, 112 leaves, 4 steps):

$$\frac{g (ex + d)^2 \operatorname{erfi} \left(\frac{\frac{1}{n} + a b f \ln(F) + b^2 f \ln(F) \ln(c (ex + d)^n)}{b \sqrt{f} \sqrt{\ln(F)}} \right) \sqrt{\pi}}{2 b e e^{\frac{1 + 2 a b f n \ln(F)}{b^2 f n^2 \ln(F)}} n (c (ex + d)^n)^{\frac{2}{n}} \sqrt{f} \sqrt{\ln(F)}}$$

Result(type 8, 31 leaves):

$$\int F^{f(a + b \ln(c (ex + d)^n))^2} (egx + gd) dx$$

Problem 161: Unable to integrate problem.

$$\int F^{f(a + b \ln(c (ex + d)^n))^2} dx$$

Optimal(type 4, 111 leaves, 4 steps):

$$\frac{(ex + d) \operatorname{erfi} \left(\frac{\frac{1}{n} + 2 a b f \ln(F) + 2 b^2 f \ln(F) \ln(c (ex + d)^n)}{2 b \sqrt{f} \sqrt{\ln(F)}} \right) \sqrt{\pi}}{2 b e e^{\frac{1 + 4 a b f n \ln(F)}{4 b^2 f n^2 \ln(F)}} n (c (ex + d)^n)^{\frac{1}{n}} \sqrt{f} \sqrt{\ln(F)}}$$

Result(type 8, 22 leaves):

$$\int F^{f(a + b \ln(c (ex + d)^n))^2} dx$$

Problem 162: Unable to integrate problem.

$$\int \frac{F^{f(a + b \ln(c (ex + d)^n))^2}}{(egx + gd)^3} dx$$

Optimal(type 4, 114 leaves, 4 steps):

$$\frac{(c (ex + d)^n)^{\frac{2}{n}} \operatorname{erfi} \left(\frac{\frac{1}{n} - a b f \ln(F) - b^2 f \ln(F) \ln(c (ex + d)^n)}{b \sqrt{f} \sqrt{\ln(F)}} \right) \sqrt{\pi}}{2 b e e^{\frac{1 - 2 a b f n \ln(F)}{b^2 f n^2 \ln(F)}} g^3 n (ex + d)^2 \sqrt{f} \sqrt{\ln(F)}}$$

Result(type 8, 33 leaves):

$$\int \frac{F^{f(a + b \ln(c (ex + d)^n))^2}}{(egx + gd)^3} dx$$

Problem 211: Unable to integrate problem.

$$\int f^{a+bx^n} g^{c+dx^n} dx$$

Optimal(type 4, 50 leaves, 2 steps):

$$\frac{f^a g^c x \Gamma\left(\frac{1}{n}, -x^n (b \ln(f) + d \ln(g))\right)}{n (-x^n (b \ln(f) + d \ln(g)))^{\frac{1}{n}}}$$

Result(type 8, 21 leaves):

$$\int f^{a+bx^n} g^{c+dx^n} dx$$

Problem 212: Unable to integrate problem.

$$\int f^{(bx+a)^n} (bx+a)^m dx$$

Optimal(type 4, 57 leaves, 1 step):

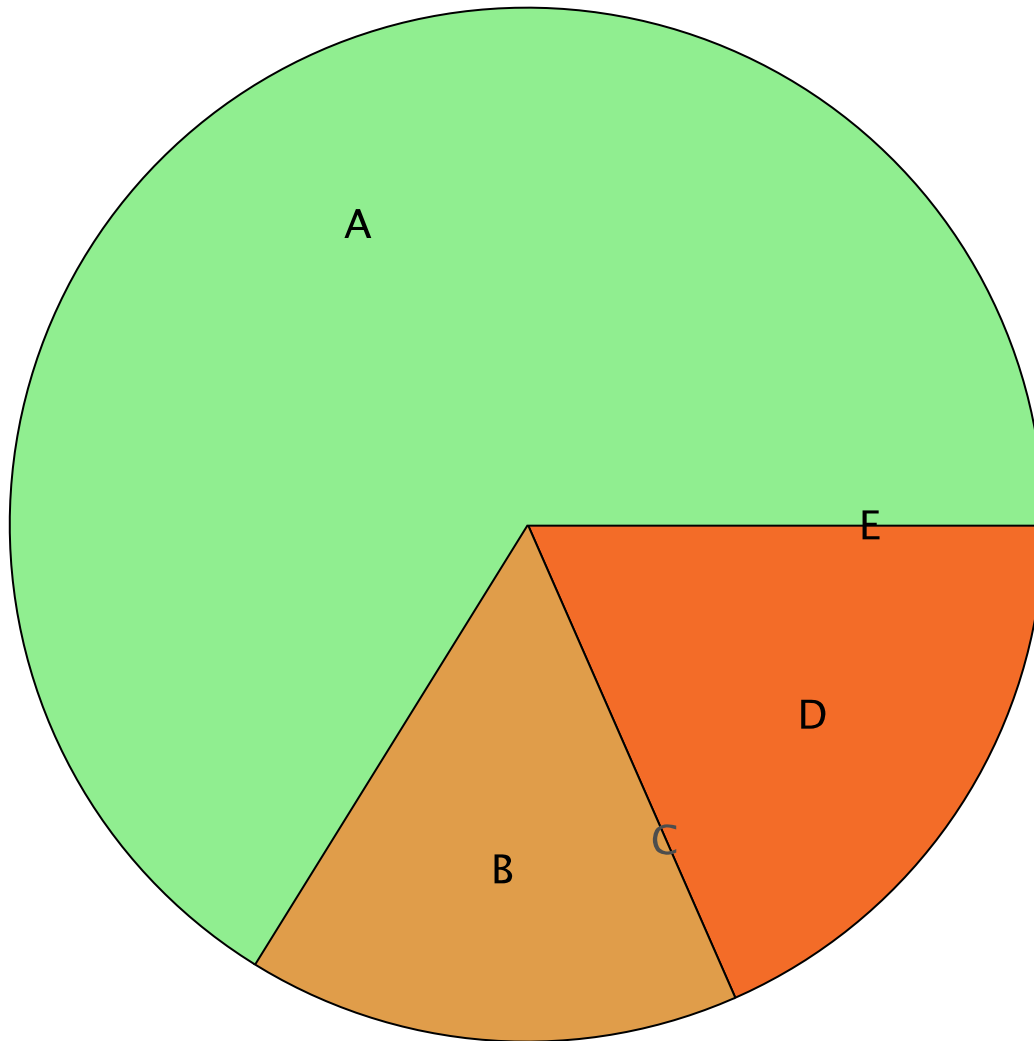
$$\frac{(bx+a)^{1+m} \Gamma\left(\frac{1+m}{n}, -(bx+a)^n \ln(f)\right)}{bn (-(bx+a)^n \ln(f))^{\frac{1+m}{n}}}$$

Result(type 8, 19 leaves):

$$\int f^{(bx+a)^n} (bx+a)^m dx$$

Summary of Integration Test Results

266 integration problems



A - 176 optimal antiderivatives
B - 41 more than twice size of optimal antiderivatives
C - 0 unnecessarily complex antiderivatives
D - 49 unable to integrate problems
E - 0 integration timeouts